

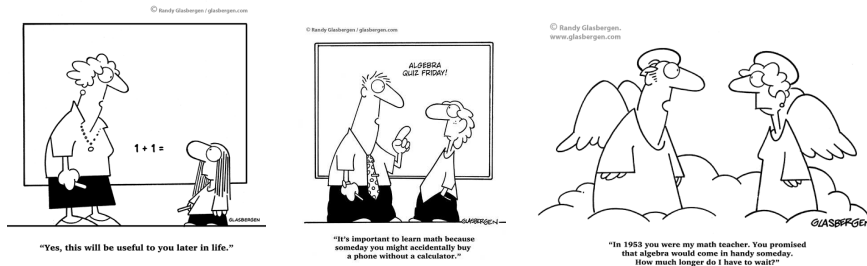
Foundations of Computer Science

Lecture 1

Warmup: A Taste for Discrete Math and Computing

Background

Disease spread, speed-dating, friendship networks



(Today) Warmup: A Taste for Discrete Math and Computing

- 1 Resources and Rules
- 2 Storyline
- 3 Background
- 4 A Taste of Discrete Math
 - Two-Contact Ebola on a Grid
 - Scheduling Speed Dates
 - Friendship Networks and Ads
 - Modeling Computers
- 5 Getting Good at Discrete Math
 - Computing is Mathematics
 - Polya's Mouse

Adapted from Malik Magdon-Ismael

Warmup: A Taste for Discrete Math and Computing: 2 / 12

Resources and Rules →

Resources and Rules

- 1 **Web Page:** www.cs.rpi.edu/~gittea/old-site/teaching/fall2026/focs.html
 - syllabus: [.../fall_2026_focs_syllabus.pdf](#)
 - schedule+reading+slides: [.../readings.html](#)
 - assignments+exams: [.../assignments.html](#)
- 2 **Text Book:** *Discrete Mathematics and Computing* (Magdon-Ismael).
- 3 **Piazza** for all discussion and announcements.
Submitty for homework: pdf only, 10MB limit.
- 4 **Instructors:** Clayton Thomas, Alex Gittens.
- 5 **5 TAs, 5 UG-Mentors.** Help session Sundays 2–6pm, AE 118.
- 6 **Recitations:** Wednesdays, Low CII 4034/4040.
- 7 **Prerequisites:**
 - CSCI 1200 (data structures)
 - MATH 1010 (Calc I) MATH 1020 (Calc II **STRONGLY** recommended)
- 8 **Rules:** No food, no electronics, no cheating, **no LLMs** on gradeables.

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Warmup: A Taste for Discrete Math and Computing: 3 / 12

The Storyline →

The Storyline

- 1 Discrete objects.
- 2 Reasoning about discrete objects
- 3 Counting discrete objects
- 4 Randomness: probability
- 5 What can we compute?
- 6 What can we compute efficiently?

■ concepts/concrete
■ proof/theory/abstract
■ theory of computation

our language will be mathematics ...
... it will be everywhere

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Warmup: A Taste for Discrete Math and Computing: 4 / 12

Background →

Background

Programming, numbers, geometry, algebra, calculus, ...

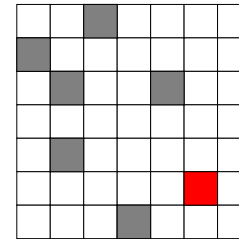
- What is the minimum element in the set $\{8, 9, 3, 10, 19\}$?
- Does this set of *positive* numbers have a minimum element:

$\{25, 97, 107, 100, 18, 33, 99, 27, 2014, 2200, 23, \dots\}$

Any (non-empty) set containing only **positive integers** has a minimum element.

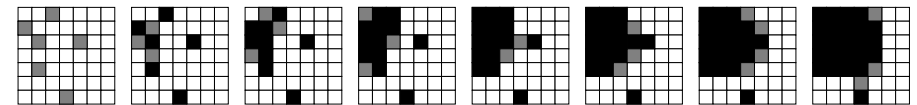
Two-Contact Ebola on a Grid

A square gets infected if two or more neighbors (N,S,E,W) are infected.



- Given initial gray infections, who ultimately gets infected?
- Minimum infections to infect everyone?
- Given few vaccines, who to immunize?
- What were the “entry points”?

Answers involve discrete math.



day 1

day 2

day 3

day 4

day 5

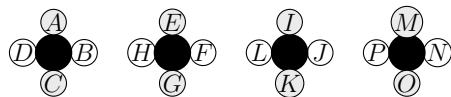
day 6

day 7

day 8

Scheduling Speed Dates

In each round 4 people “group”-speed-date around a table. (4 rounds in all)



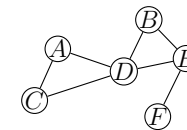
How to organize the rounds so that people meet as many people as possible?

- Do you care about average or minimum number of meetups per person?
- Can everyone meet at least 10 people?
- What happens if you assign tables randomly?

Answers involve discrete math.

Friendship Networks and Ads

People are circles and links are friendships.



Who would you advertise to? You wish to maximize adoption of your new technology.

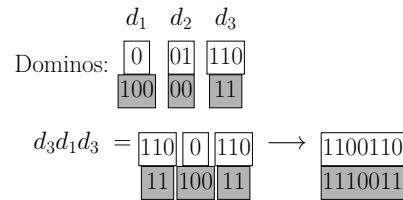
Answers involve discrete math.

Desktop, smartphone, fitbit, ...

We have deep questions:

- ❶ What can we compute?
- ❷ What *can't* we compute?
- ❸ How fast?

What is computing?



Domino puzzle: Want same top and bottom.

Domino program:

Input: dominoes

Output: sequence that works

or

say it can't be done

Answers involve discrete math.

"Too few people recognize that the high technology so celebrated today is essentially a mathematical technology."

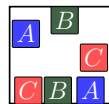
"A programmer must *demonstrate* that their program has the required properties. If this comes as an afterthought, it is all but certain that they won't be able to meet this obligation. Only if this obligation influences the design is there hope to meet it. . .

"The required techniques of effective reasoning are pretty formal, but as long as programming is done by people who don't master them, the software crisis will remain with us and will be considered an incurable disease. And you know what incurable diseases do: they invite the quacks and charlatans in, who in this case take the form of Software Engineering Gurus."

– Edsger Dijkstra

Polya's Mouse

"A mouse tries to escape from an old fashioned cage. After many futile attempts bouncing back-and-forth, thumping his body against the cage bars, he finally finds one place where the bars are *slightly* wider apart. The mouse, bruised and battered escapes through this small opening, and to his elation, finds freedom." – Polya



Connect tiles of the same letter with wires. Wires cannot cross, enter tiles, or leave the box. How can it be done? If it can't be done, why not?

Don't be quick to dismiss either conclusion. Try this and that. Fiddle around until you understand the problem and the difficulty. Patience.

To solve such problems, "*You need brains and good luck. But, you must also sit tight and wait till you get a bright idea.*" – Polya.

Getting Good at Discrete Math

The *professional's* workflow in addressing a discrete math problem:

- 1: Model the problem you are trying to solve using a discrete mathematical object.
- 2: Tinker with easy cases to build an understanding of the model.
- 3: Based on the tinkering, formulate a conjecture about your problem/model.
- 4: Prove the conjecture and make it a theorem. You now *know* something new.

Tinker, Tinker, Tinker,

Tinker!

