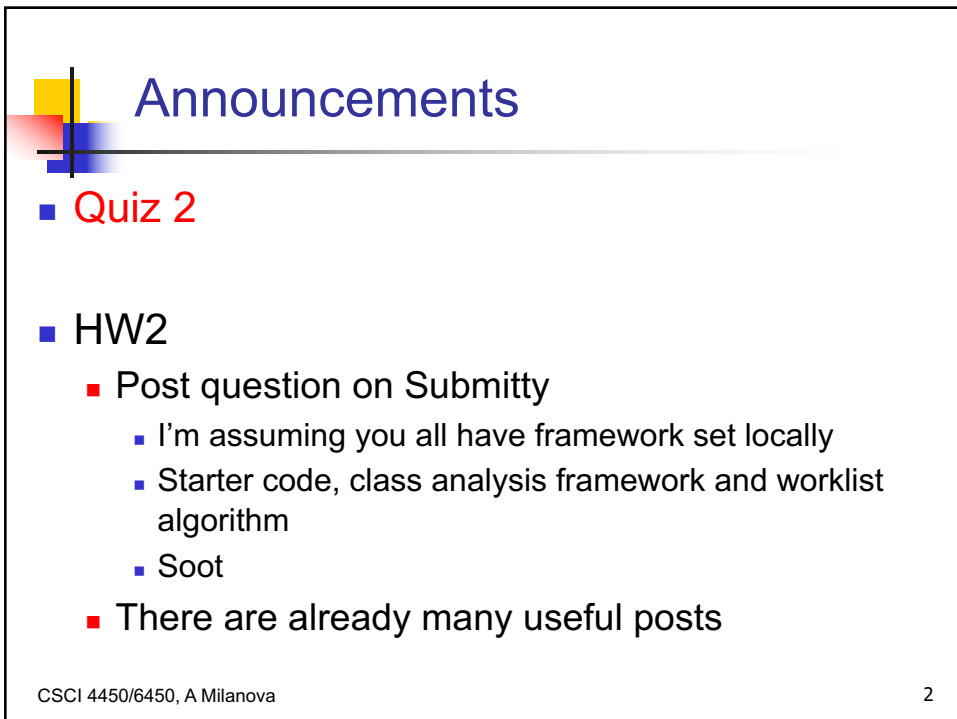



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Outline of Today's Class

- Rapid Type Analysis (RTA), last time
- HW2, Class analysis framework questions?
- The XTA analysis family
 - 0-CFA
 - Points-to analysis (PTA)

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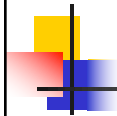


Class Analysis

- Problem statement: What are the **classes** of objects that a (Java) **reference** variable may refer to?
- Applications
 - Call graph construction
 - Nodes are method
 - Edges represent calls
 - Notion of methods reachable from **main**
 - Virtual call resolution

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RTA, A Declarative Specification

R is the set of **reachable methods**

I is the set of **instantiated types**

1. $\{ \text{main} \} \subseteq \mathbf{R}$ // Algo: initialize **R** with **main**

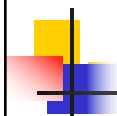
2. for each method $\mathbf{m} \in \mathbf{R}$ and
each **new site new C** in **m**

$\{ \mathbf{C} \} \subseteq \mathbf{I}$ // Algo: add **C** to **I**; schedule
// “successor” constraints

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RTA, A Declarative Specification

3. for each method $\mathbf{m} \in \mathbf{R}$,
each **virtual call** $\mathbf{y.n(z)}$ in **m**,
each class **C** in $\mathbf{SubTypes(StaticType(y))} \cap \mathbf{I}$,
and $\mathbf{n'}$, where $\mathbf{n'} = \mathbf{resolve(C,n)}$

$\{ \mathbf{n'} \} \subseteq \mathbf{R}$ // Algo: add target $\mathbf{n'}$ to **R**, if not already
// there. Schedule “successors”

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Worklist Algorithm for Flow-Insensitive Analysis

- Flow-insensitive, context-insensitive analysis

```
S = ... /* initialize S, typically to empty, which is 0 of lattice */
W = { f1, ... fn } /* initialize W with transfer functions in main */
while W ≠ ∅ do {
    remove fj from W
    S = fj(S) /* fj never "kills" */
    if S changed
        W = W U Successors
/* Successors includes all affected transfer functions; easy safe
approximation for us: include all fj's in reachable methods */
}
```

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XTA Analysis Family

- Due to Tip and Palsberg
 - Frank Tip and Jens Palsberg, “Scalable Propagation-Based Call Graph Construction Algorithms”, OOPSLA '00
- Generalizes RTA
- Improves on RTA by keeping more info
 - What if we kept sets per method and per field rather than a “blob” I?

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XTA

R is the set of **reachable methods**


S_m is the set of **types** that flow to method **m**

S_f is the set of **types** that flow to field **f**

1. $\{ \text{main} \} \subseteq \mathbf{R}$
2. for each method $\mathbf{m} \in \mathbf{R}$ and each **new site new C** in **m**

$$\{ \mathbf{C} \} \subseteq \mathbf{S}_m$$

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XTA

3. for each method $\mathbf{m} \in \mathbf{R}$, each **virtual call y.n(z)** in **m**, each class **C** in $\mathbf{SubTypes}(\mathbf{StaticType}(y)) \cap \mathbf{S}_m$ and **n'**, where $\mathbf{n}' = \mathbf{resolve}(\mathbf{C}, \mathbf{n})$
 - $\{ \mathbf{n}' \} \subseteq \mathbf{R}$ // add **n'** to **R** if not already there
 - $\{ \mathbf{C} \} \subseteq \mathbf{S}_{\mathbf{n}'}$ // add **C** to **S_{n'}** if not already there
 - $\mathbf{S}_m \cap \mathbf{SubTypes}(\mathbf{StaticType}(p)) \subseteq \mathbf{S}_{\mathbf{n}'}$
 - $\mathbf{S}_{\mathbf{n}'} \cap \mathbf{SubTypes}(\mathbf{StaticType}(\mathbf{ret})) \subseteq \mathbf{S}_m$

(**p** denotes the parameter of **n'**, and **ret** denotes the return of **n'**)

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XTA

4. for each method $m \in R$,
each field read $x = y.f$ in m
 $S_f \sqsubseteq S_m$

5. for each method $m \in R$,
each field write $x.f = y$ in m
 $S_m \cap \text{SubTypes}(\text{StaticType}(f)) \sqsubseteq S_f$

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Practical Concerns

- Multiple parameters
- Direct calls
 - either **static invoke** calls or
 - **special invoke** calls
- Array reads and writes!
- Static fields

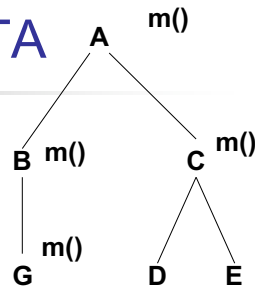
- See Tip and Palsberg for more

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Example: RTA vs. XTA

```
public class Main {
    public static void main() {
        n1();
        n2();
    }
    static void n1() {
        A a1 = new B();
        a1.m();
    }
    static void n2() {
        A a2 = new C();
        a2.m();
    }
}
```



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Boolean Expression Hierarchy: RTA vs. XTA vs. "Ground Truth"

```
public class AndExp extends BoolExp {
    private BoolExp left;
    private BoolExp right;

    public AndExp(BoolExp left, BoolExp right) {
        this.left = left;
        this.right = right;
    }

    public boolean evaluate(Context c) {
        private BoolExp l = this.left;
        private BoolExp r = this.right;
        return l.evaluate(c) && r.evaluate(c);
    }
}
```

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Boolean Expression Hierarchy: RTA vs. XTA vs. "Ground Truth"

```
public class OrExp extends BoolExp {
    private BoolExp left;
    private BoolExp right;

    public OrExp(BoolExp left, BoolExp right) {
        this.left = left;
        this.right = right;
    }
    public boolean evaluate(Context c) {
        private BoolExp l = this.left;
        private BoolExp r = this.right;
        return l.evaluate(c) || r.evaluate(c);
    }
}
```

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Boolean Expression Hierarchy: RTA vs. XTA vs. "Ground Truth"

```
main() {
    Context theContext = new Context();
    BoolExp x = new VarExp("X");
    BoolExp y = new VarExp("Y");
    BoolExp exp = new AndExp(
        new Constant(true), new OrExp(x, y) );
    theContext.assign(x, true);
    theContext.assign(y, false);
    boolean result = exp.evaluate(theContext);
}
```

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Outline of Today's Class

- Rapid Type Analysis (RTA), last time
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 - **0-CFA**
 - Points-to analysis (PTA)

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0-CFA

- Described in Tip and Palsberg's paper
- 0-CFA stands for 0-level Control Flow Analysis, where "0-level" stands for **context-insensitive** analysis
 - Will see 1-CFA, 2-CFA, ... k-CFA later
- Improves on XTA by storing even more information about flow of class types

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0-CFA

R is the set of **reachable methods**

S_v is the set of **types** that flow to variable v


S_f is the set of **types** that flow to field **f**

1. $\{ \text{main} \} \subseteq \mathbf{R}$
2. for each method $\mathbf{m} \in \mathbf{R}$ and each **new site** $\mathbf{x} = \text{new } \mathbf{C}$ in \mathbf{m}

$$\{ \mathbf{C} \} \subseteq \mathbf{S}_x$$

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0-CFA

3. for each method $\mathbf{m} \in \mathbf{R}$, each **virtual call** $\mathbf{x} = \mathbf{y}.\mathbf{n}(\mathbf{z})$ in \mathbf{m} , each class \mathbf{C} in \mathbf{S}_y and \mathbf{n}' , where $\mathbf{n}' = \text{resolve}(\mathbf{C}, \mathbf{n})$

$$\{ \mathbf{n}' \} \subseteq \mathbf{R}$$

$$\{ \mathbf{C} \} \subseteq \mathbf{S}_{\text{this}}$$


$$\mathbf{S}_z \cap \text{SubTypes}(\text{StaticType}(\mathbf{p})) \subseteq \mathbf{S}_p$$

$$\mathbf{S}_{\text{ret}} \cap \text{SubTypes}(\text{StaticType}(\mathbf{x})) \subseteq \mathbf{S}_x$$

(**this** is the implicit parameter of \mathbf{n}' , \mathbf{p} is the parameter of \mathbf{n}' , and **ret** is the return of \mathbf{n}')

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0-CFA

4. for each method $m \in R$,
each **field read** $x = y.f$ in m
 $S_f \cap \text{SubTypes}(\text{StaticType}(x)) \sqsubseteq S_x$

5. for each method $m \in R$,
each **field write** $x.f = y$ in m
 $S_y \cap \text{SubTypes}(\text{StaticType}(f)) \sqsubseteq S_f$

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0-CFA

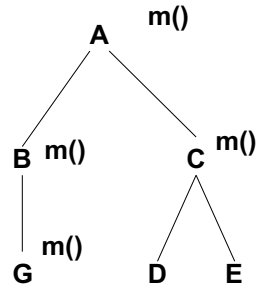
6. for each method $m \in R$,
each **assignment** $x = y$ in m
 $S_y \cap \text{SubTypes}(\text{StaticType}(x)) \sqsubseteq S_x$

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Example: XTA vs. 0-CFA

```
public class Main {  
    public static void main() {  
        A a1 = new B();  
        a1.m();  
  
        A a2 = new C();  
        a2.m();  
    }  
}
```



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Boolean Expression Hierarchy: XTA vs. 0-CFA

```
public class AndExp extends BoolExp {  
    private BoolExp left;  
    private BoolExp right;  
  
    public AndExp(BoolExp left, BoolExp right) {  
        this.left = left;  
        this.right = right;  
    }  
  
    public boolean evaluate(Context c) {  
        private BoolExp l = this.left;  
        private BoolExp r = this.right;  
        return l.evaluate(c) && r.evaluate(c);  
    }  
}
```

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Boolean Expression Hierarchy: XTA vs. 0-CFA

```
public class OrExp extends BoolExp {
    private BoolExp left;
    private BoolExp right;

    public OrExp(BoolExp left, BoolExp right) {
        this.left = left;
        this.right = right;
    }
    public boolean evaluate(Context c) {
        private BoolExp l = this.left;
        private BoolExp r = this.right;
        return l.evaluate(c) || r.evaluate(c);
    }
}
```

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Boolean Expression Hierarchy: XTA vs. 0-CFA

```
main() {
    Context theContext = new Context();
    BoolExp x = new VarExp("X");
    BoolExp y = new VarExp("Y");
    BoolExp exp = new AndExp(
        new Constant(true), new OrExp(x, y) );
    theContext.assign(x, true);
    theContext.assign(y, false);
    boolean result = exp.evaluate(theContext);
}
```

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Outline of Today's Class

- Rapid Type Analysis (RTA), last time
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 - **Points-to analysis (PTA)**

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PTA

- Widely referred to as Andersen's points-to analysis for Java
- Improves on 0-CFA by storing information about **objects**, not classes
 - `A a1 = new A(); // o1`
 - `A a2 = new A(); // o2`

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PTA

R is the set of **reachable methods**

Pt(v) is the set of **objects** that **v** may point to


Pt(o.f) is the set of **objects** that field **f** of object **o** may point to

1. $\{ \text{main} \} \subseteq \mathbf{R}$
2. for each method $m \in \mathbf{R}$ and each **new site** $i: x = \text{new } \mathbf{C}$ in m

$$\{ o_i \} \subseteq \mathbf{Pt}(x) \text{ // instead of } \mathbf{C}, \text{ we have } o_i$$

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PTA

class_of(o) returns the class of object **o**

3. for each method $m \in \mathbf{R}$, each **virtual call** $x = y.n(z)$ in m , each class o_i in **Pt(y)** and n' , where $n' = \text{resolve}(\text{class_of}(o_i), n)$

$$\{ n' \} \subseteq \mathbf{R}$$

$$\{ o_i \} \subseteq \mathbf{Pt}(\text{this})$$


$$\mathbf{Pt}(z) \cap \text{SubTypes}(\text{StaticType}(p)) \subseteq \mathbf{Pt}(p)$$

$$\mathbf{Pt}(\text{ret}) \cap \text{SubTypes}(\text{StaticType}(x)) \subseteq \mathbf{Pt}(x)$$

(**this** is the implicit parameter of n' , **p** is the parameter of n' , and **ret** is the return of n')

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PTA

4. for each method $m \in R$,
 each **field read** $x = y.f$ in m
 for each object $o \in Pt(y)$
 $Pt(o.f) \cap SubTypes(StaticType(x)) \sqsubseteq Pt(x)$

5. for each method $m \in R$,
 each **field write** $x.f = y$ in m
 for each object $o \in Pt(x)$
 $Pt(y) \cap SubTypes(StaticType(f)) \sqsubseteq Pt(o.f)$

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PTA

6. for each method $m \in R$,
 each **assignment stmt** $x = y$ in m
 $Pt(y) \cap SubTypes(StaticType(x)) \sqsubseteq Pt(x)$

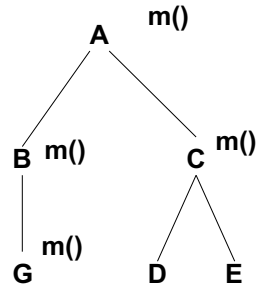
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Example: 0-CFA vs. PTA

```
public class Main {  
  public static void main() {  
    X x1 = new X(); // o1  
    A a1 = new B(); // o2  
    x1.f = a1; // o1.f points to o2  
    A a2 = x1.f; // a2 points to o2  
    a2.m();  
  
    X x2 = new X(); // o3  
    A a3 = new C(); // o4  
    x2.f = a3; // o3.f points to o4  
    A a4 = x2.f; // a4 points to o4  
    a4.m();  
  }  
}
```



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Big Picture

- All fit into our monotone dataflow framework!
- Flow-insensitive, context-insensitive
 - Compute single solution S
- Algorithms differ mainly in “size” of S
 - RTA: only 2 kinds of statements; Lattice?
 - XTA: expands to all statements; Lattice?
 - 0-CFA: all statements; Lattice?
 - PTA (Points-to analysis): all statements; Lattice elements are points-to graphs

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The Big Picture

RTA:

Types: A B C D

XTA:

A B C D ...

0-CFA:

A B C D ...

PTA:

o₁:A o₂:A o₃:B o₄:B o₅:C o₆:D ...

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