

QUIZ 3: 60 Minutes

Last Name: _____

First Name: _____

RIN: _____

Section: _____

Answer **ALL** questions.

NO COLLABORATION or electronic devices. Any violations result in an **F**.
NO questions allowed during the test. Interpret and do the best you can.

GOOD LUCK!

Circle at most one answer per question.

10 points for each correct answer

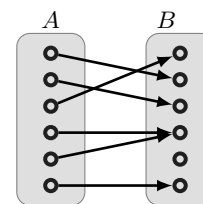
You **MUST** show **CORRECT** work to get full credit.

When in doubt, **TINKER**.

Total
200

1. Which describes the function on the right that maps A to B .

- A f is not an injection (1-to-1) and f is not a surjection (onto).
- B f is an injection (1-to-1) and f is not a surjection (onto).
- C f is not an injection (1-to-1) and f is a surjection (onto).
- D f is an injection (1-to-1) and f is a surjection (onto).
- E None of the above.



2. A set \mathcal{S} contains all the distinct functions which map $\{0, 1\}$ to \mathbb{N} . What is the cardinality of \mathcal{S} ?

- A 0.
- B 1.
- C Bigger than 1 but finite.
- D The same as $|\mathbb{N}|$.
- E Strictly larger than $|\mathbb{N}|$.

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4. What is a computing problem?

- A A person who knows how to write a program in python.
- B A machine that transitions between states.
- C A rule for deciding if a string belongs to a set.
- D Any set of finite binary strings.
- E A Turing Machine.

5. Which set is *not* countable, i.e., has a cardinality strictly larger than $|\mathbb{N}|$?

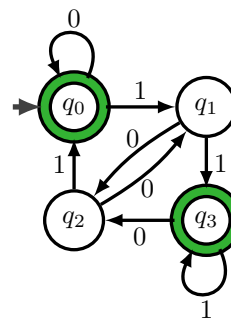
- A \mathbb{Q} , the rational numbers.
- B All distinct finite binary strings.
- C All possible Turing Machines.
- D All possible computing problems.
- E They are all countable.

6. The language $\mathcal{L} = \{11, 111\}^*$ (Kleene star). Which string is not in \mathcal{L} ?

- A ε .
- B 1.
- C 1111.
- D 11111.
- E They are all in \mathcal{L} .

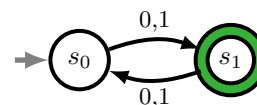
7. What is the final resting state for the DFA on input 110110.

- A q_0 .
- B q_1 .
- C q_2 .
- D q_3 .
- E None of the above



8. Let $\Sigma = \{0, 1\}$. Which regular expression is the problem solved by the DFA.

- A Σ^* .
- B $\Sigma \cdot \Sigma \cdot \Sigma$.
- C $(\Sigma \cdot \Sigma) \cdot \Sigma^*$.
- D $\Sigma \cdot (\Sigma \cdot \Sigma)^*$.
- E None of the above.



9. How many 5 bit strings are in the YES-set of the DFA in problem 8.

- A 4.
- B 8.
- C 16.
- D 32.
- E None of the above.

10. Which computing problem *cannot* be solved by a DFA (deterministic finite automata)?

- A $\mathcal{L} = \{\text{strings with no 1s}\}$.
- B $\mathcal{L} = \{\text{strings with an odd number of 1s}\}$.
- C $\mathcal{L} = \{\text{strings that are not 1111}\}$.
- D $\mathcal{L} = \{\text{strings with more 1s than 0s}\}$.
- E Each problem above can be solved by a DFA.

11. The main limitation of the DFA which prevents it from solving $\mathcal{L} = \{0^n 1^{n+3} | n \geq 0\}$ is:

- A The DFA can't have more than one yes-state.
- B The input string can be arbitrarily long.
- C The DFA can go into an infinite loop.
- D The DFA cannot remember how many 0s have gone by because it has only finitely many states.
- E None of the above, because a DFA can solve \mathcal{L} .

12. Which string cannot be generated by the CGF shown?

1 : $S \rightarrow \varepsilon \mid A \mid B$
2 : $A \rightarrow 0 \mid 0B$
3 : $B \rightarrow 1 \mid 1A$

- A ε
- B 010
- C 101
- D 011
- E They can all be generated.

13. Which CFG generates all strings with an even number of bits, including ε .

- A $S \rightarrow \varepsilon \mid SS$
- B $S \rightarrow \varepsilon \mid 0 \mid 1 \mid SS$
- C $S \rightarrow \varepsilon \mid 01S$
- D $S \rightarrow \varepsilon \mid 00S \mid 01S \mid 10S \mid 11S$
- E None of the above.

14. Which comparison between DFAs and CFGs is correct?

- A A DFA can solve language \mathcal{L} if and only if a CFG can generate language \mathcal{L} .
- B If a DFA can solve language \mathcal{L} , then a CFG can generate language \mathcal{L} .
- C If a CFG can generate language \mathcal{L} , then a DFA can solve language \mathcal{L} .
- D There is some language \mathcal{L} which a DFA can solve, but no CFG can generate that language \mathcal{L} .
- E None of the above.

15. In the theory of computing, we define computing problems and algorithms as:

- A A computing problem is a string. An algorithm is a recognizer.
- B A computing problem is a set of finite binary strings. An algorithm is a recognizer.
- C A computing problem is a Turing Machine. An algorithm is a decider.
- D A computing problem is a set of finite binary strings. An algorithm is a person.
- E A computing problem is a set of finite binary strings. An algorithm is a decider.

16. Why do we prefer a Turing machine decider over a Turing machine recognizer?
- A Because there are some yes sets that are accepted by a decider but not a recognizer.
 - B Because a decider can write to the tape, but a recognizer cannot.
 - C Because a decider has a finite number of states, but a recognizer has infinitely many states.
 - D Because any useful algorithm should always halt giving an answer.
 - E We don't prefer one over the other because both are the same thing.
17. Consider the computing problem $\mathcal{L} = \{0^m 1^n 0^k \mid m, n, k \geq 0 \text{ and } n = m + k\}$. Which claim is not true?
- A A DFA cannot solve \mathcal{L} .
 - B A DFA with an external top-access stack memory can solve \mathcal{L} .
 - C A CFG can generate \mathcal{L} .
 - D A Turing machine decider can solve \mathcal{L} .
 - E None of the above.
18. Which problem is not solvable by an algorithm?
- A $\mathcal{L} = \{\langle M \rangle \mid M \text{ is a valid Turing Machine.}\}$
 - B $\mathcal{L} = \{0^n \mid n \geq 0\}$.
 - C $\mathcal{L} = \{0^{2^n} \mid n \geq 0\}$.
 - D Determining if any given python program correctly says if an input n is prime or not.
 - E None of the above.
19. Problem \mathcal{L}_A is reducible to \mathcal{L}_B , that is $\mathcal{L}_A \leq_R \mathcal{L}_B$. We know that \mathcal{L}_B is decidable. Which is true?
- A \mathcal{L}_A must be undecidable.
 - B \mathcal{L}_A can be undecidable.
 - C \mathcal{L}_A must be decidable.
 - D \mathcal{L}_A must be finite.
 - E None of the above.
20. Let \mathcal{M} be the set of all possible Turing Machines. Which statement is not true?
- A Every Turing Machine in \mathcal{M} can be uniquely encoded into a finite binary string.
 - B All Turing Machines in \mathcal{M} can be listed: $\{\langle M_1 \rangle, \langle M_2 \rangle, \langle M_3 \rangle, \langle M_4 \rangle, \dots, \}$.
 - C \mathcal{M} is countable.
 - D Given any computing problem \mathcal{L} , there is a Turing Machine in \mathcal{M} which solves \mathcal{L} .
 - E All of the above are true.

SCRATCH