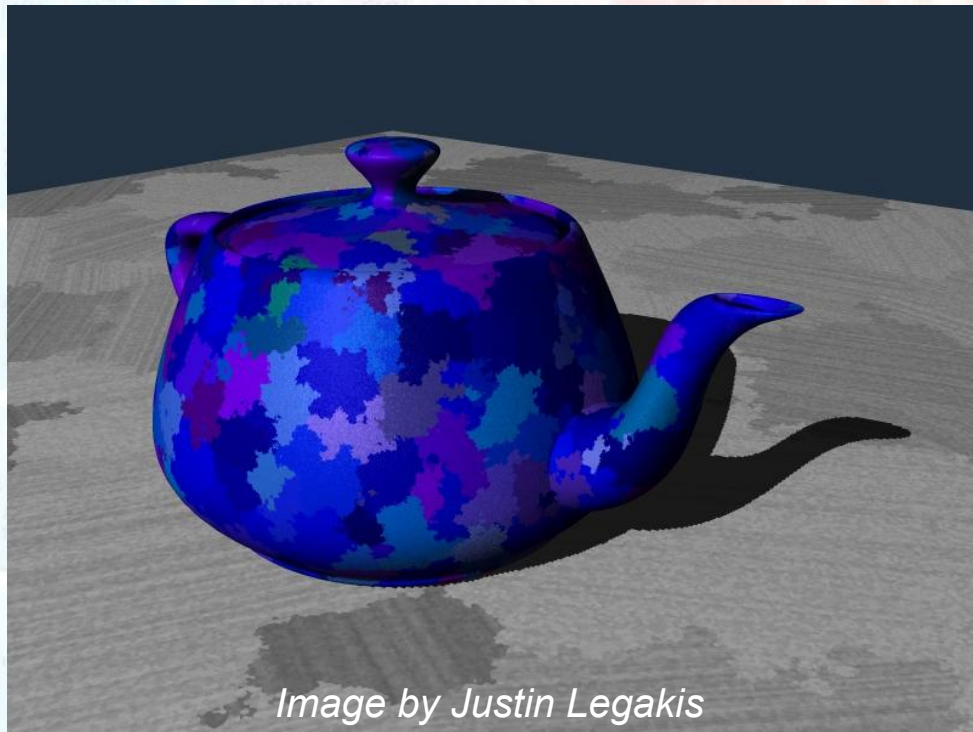


# CSCI 4530/6530 Advanced Computer Graphics

<https://www.cs.rpi.edu/~cutler/classes/advancedgraphics/S25/>

## Lecture 19: Shaders and Procedural Modeling



*Image by Justin Legakis*

*For the Birds*, Pixar, 2000

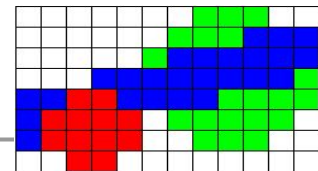
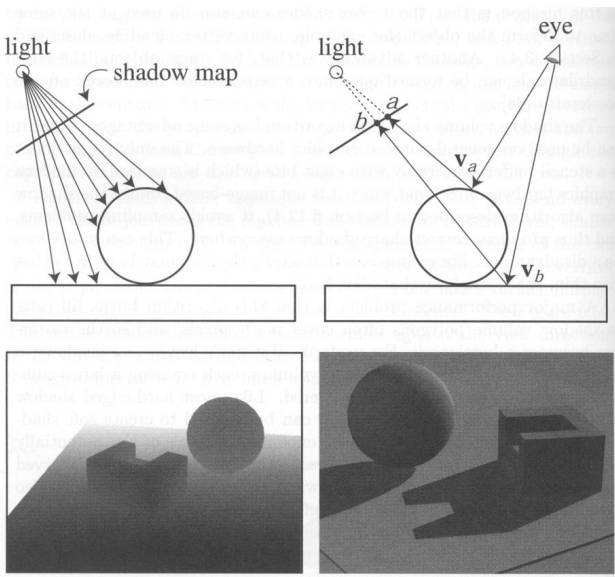
---



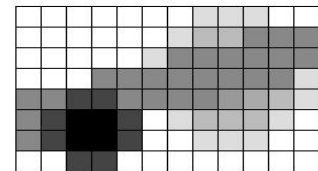


# Last Time?

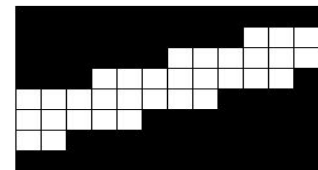
- Planar Shadows
- Projective Texture Shadows
- Shadow Maps
- Shadow Volumes
  - Stencil Buffer



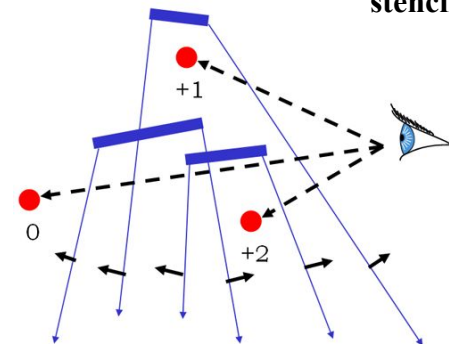
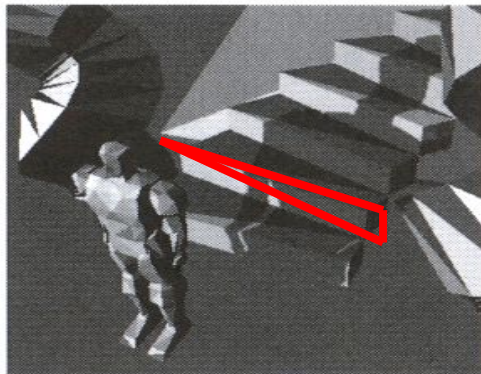
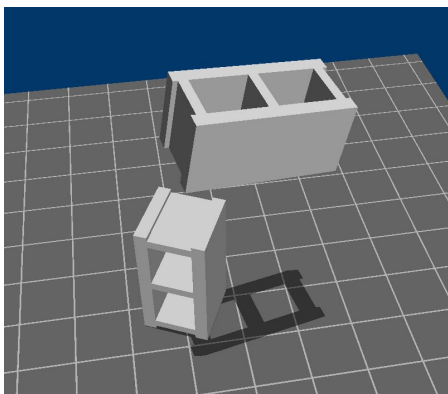
frame buffer



depth buffer



stencil buffer





# Today

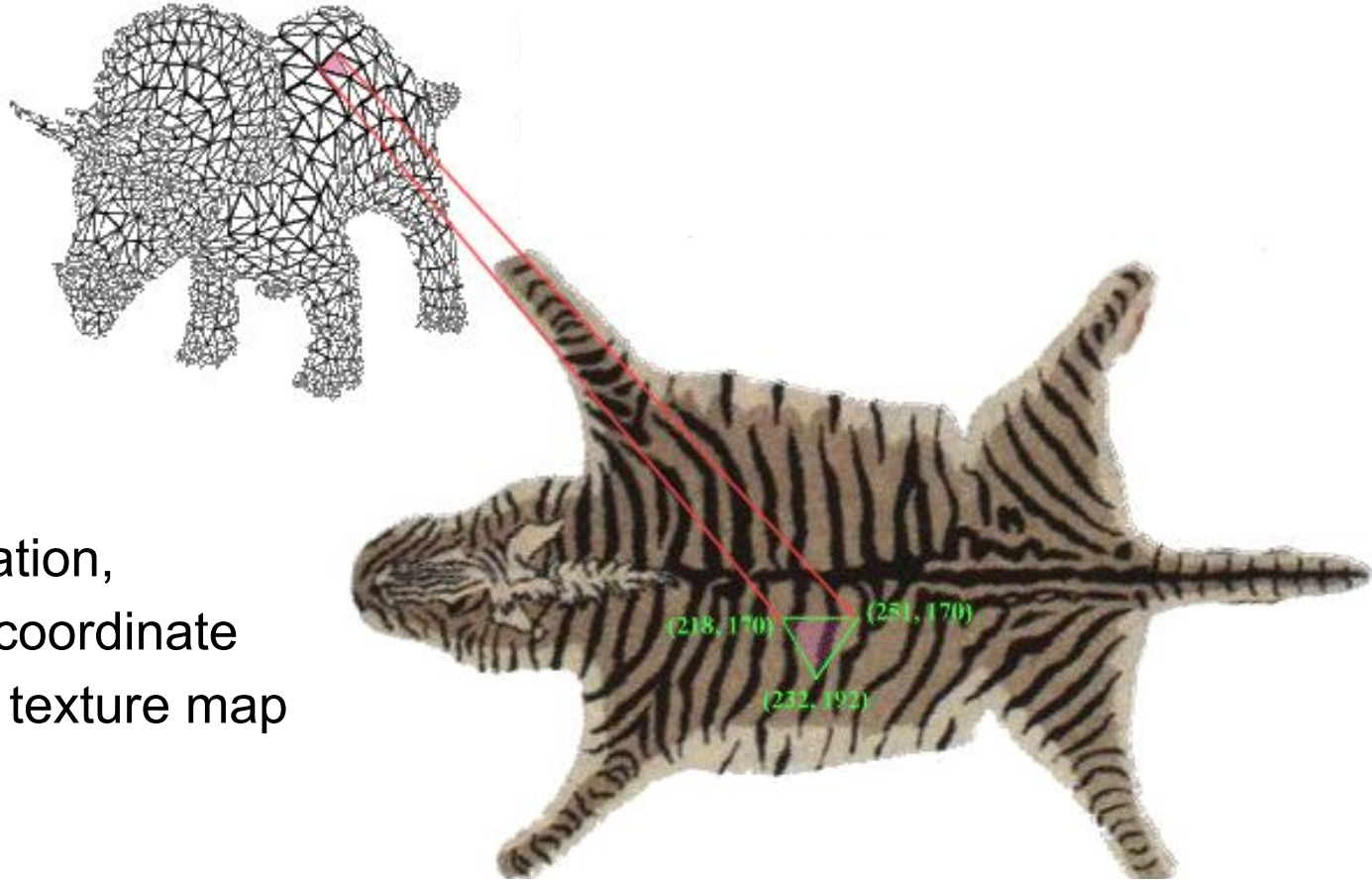
---

- **Texture Mapping & Other “Mapping” Techniques**
  - Bump Mapping
  - Displacement Mapping
  - Environment Mapping
  - Light Mapping
  - Normal Mapping
  - Parallax Mapping
  - Parallax Occlusion Mapping
- Programmable Shader Examples
  - Modern Graphics Hardware
  - Per-Pixel Shading
- Procedural Textures & Modeling
- Papers for Today
- Papers for Next Time

# Texture Mapping

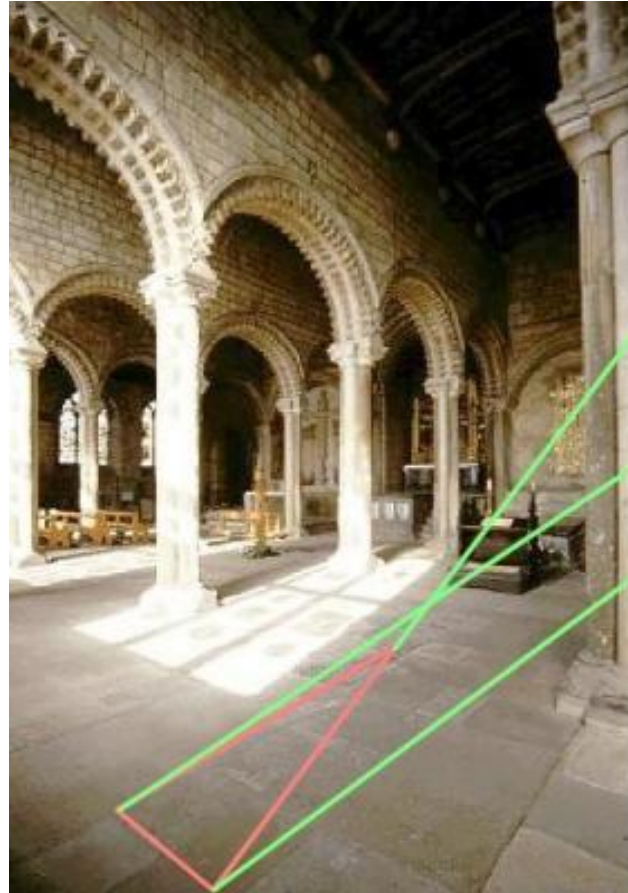
---

- For each triangle in the model, establish a corresponding region in the texture map.
- During rasterization, interpolate the coordinate indices into the texture map



# Texture Mapping Difficulties

- Tedious to specify texture coordinates
- Acquiring textures is surprisingly difficult
  - Photographs have projective distortions
  - Variations in reflectance and illumination
  - Tiling problems

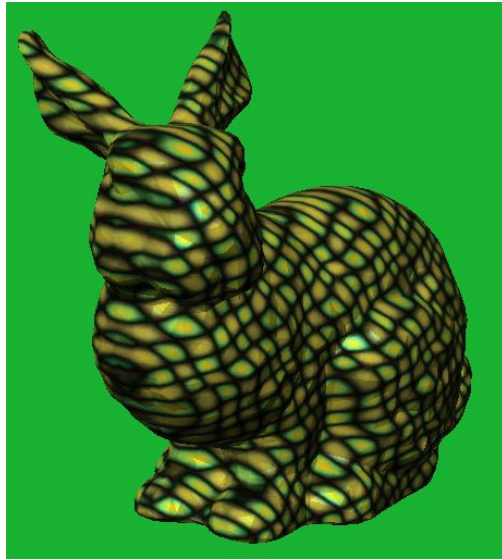


*Can't do this!*

*You can get around this problem for planar surfaces if you specify 4 points...*

# Common Texture Coordinate Mappings

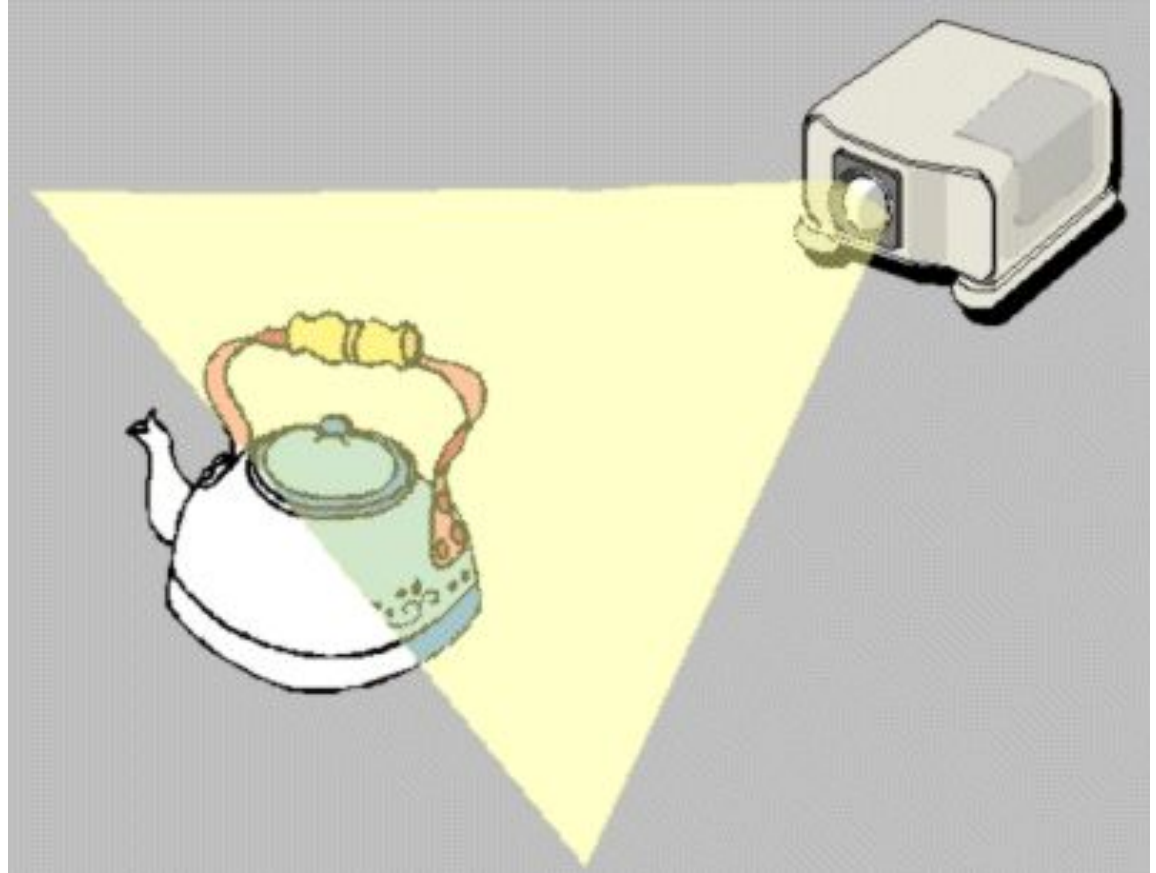
- Orthogonal
- Cylindrical
- Spherical
- Perspective Projection
- Texture Chart





# Projective Textures

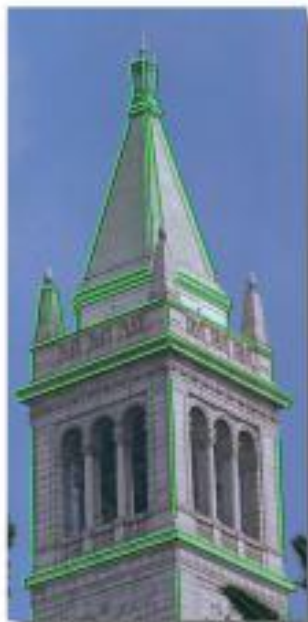
- Use the texture like a slide projector
- No need to specify texture coordinates explicitly



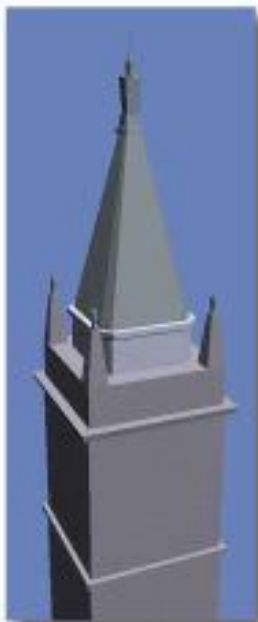
# Projective Texture Example

- Modeling from photographs
- Using input photos as textures

Figure from Debevec, Taylor & Malik  
<http://www.debevec.org/Research>



Original photograph with marked edges



Recovered model



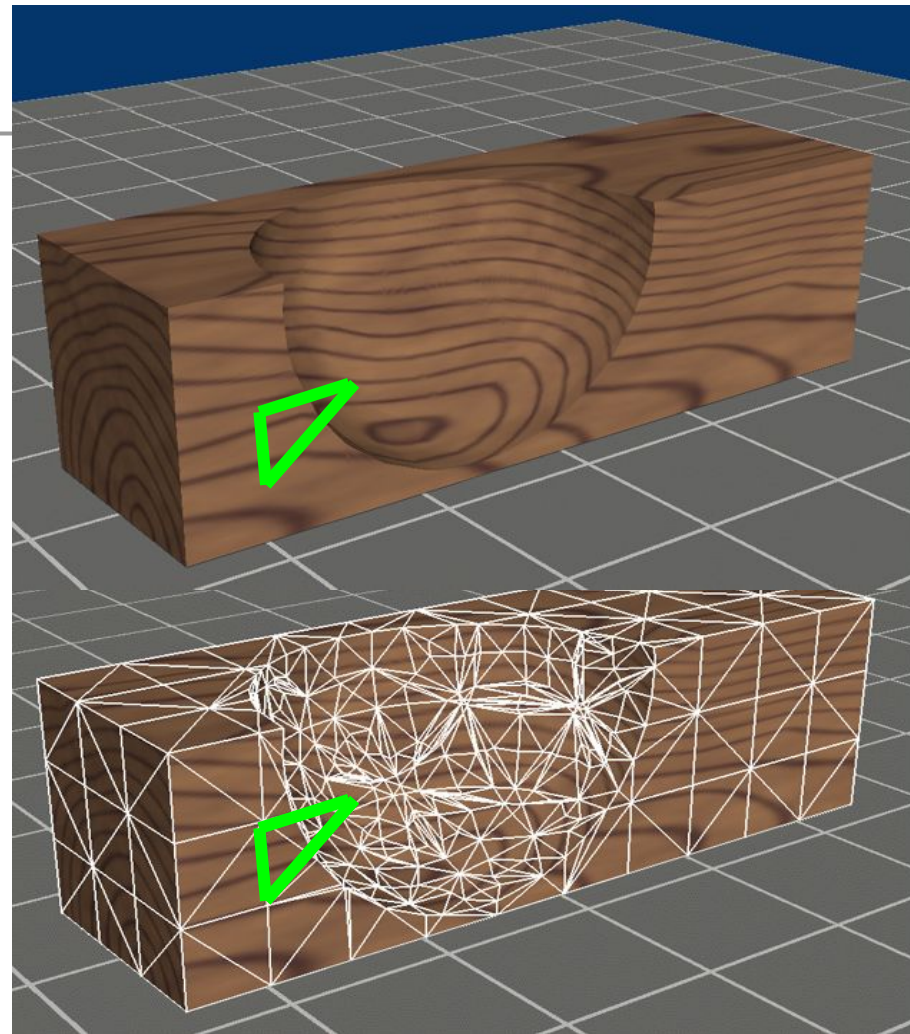
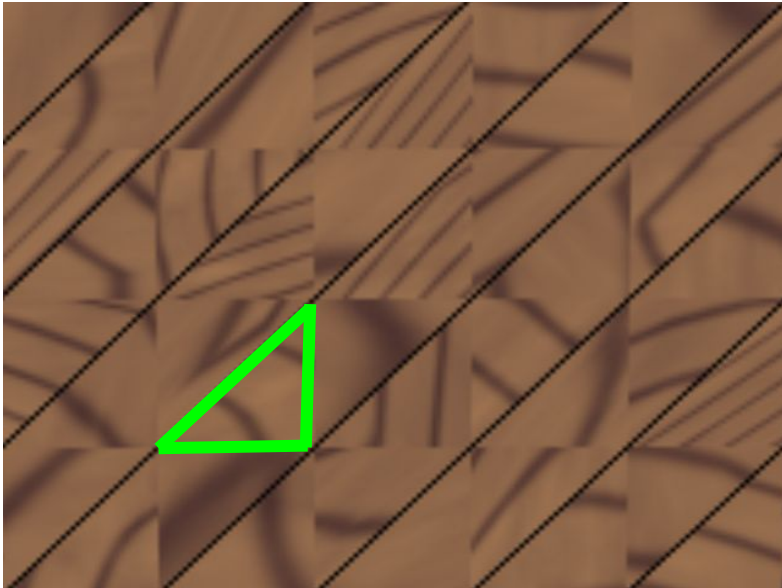
Model edges projected onto photograph



Synthetic rendering

# Texture Chart

- Pack triangles into a single image



# Today

---

- Texture Mapping & Other “Mapping” Techniques
  - **Bump Mapping**
  - Displacement Mapping
  - Environment Mapping
  - Light Mapping
  - **Normal Mapping**
  - Parallax Mapping
  - Parallax Occlusion Mapping
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  - Modern Graphics Hardware
  - Per-Pixel Shading
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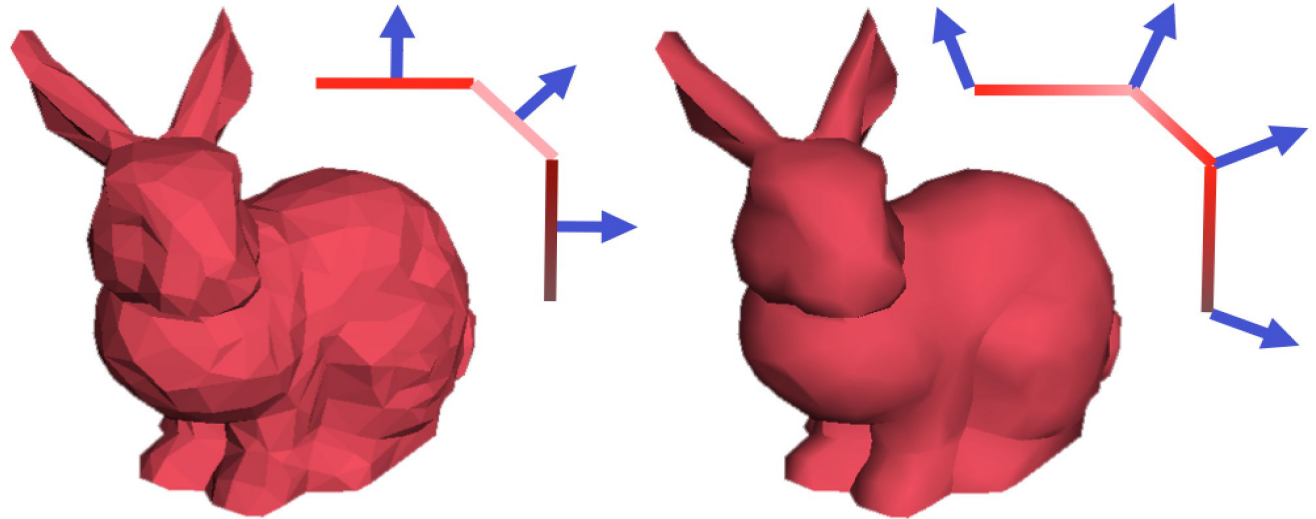


# Remember Gouraud Shading?

---

- Instead of shading with the normal of the triangle, we'll shade the vertices with the *average normal* at the vertex and *interpolate the shaded color* across each face. This gives the *illusion of a smooth surface* with smoothly varying normals.

- **Cheat normals to DISGUISE actual geometry**



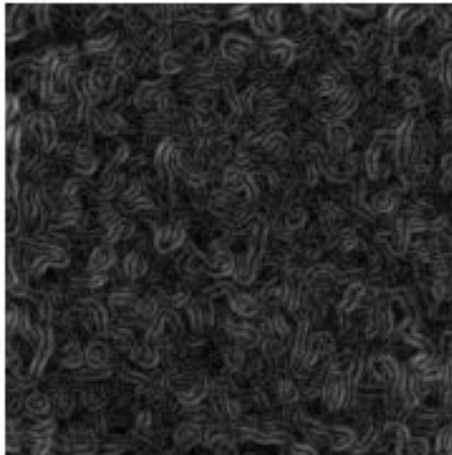
# Bump Mapping / Normal Mapping

---

- Use textures to alter the surface normal
  - Does not change the actual shape of the surface
  - Just shaded as if it were a different shape



**Sphere w/Diffuse Texture**



**Swirly Bump Map**

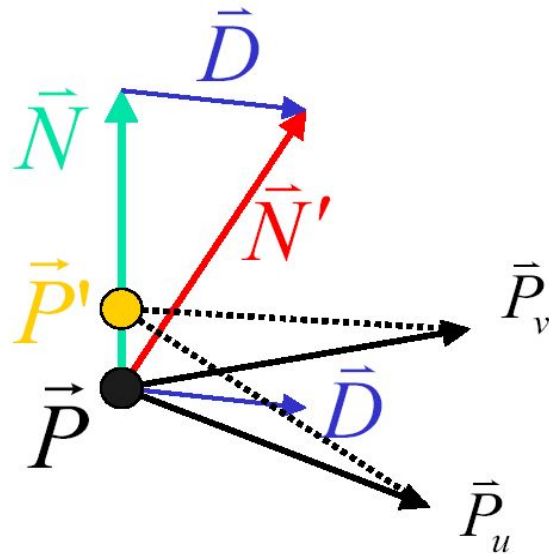


**Sphere w/Diffuse Texture  
& Bump Map**

*Cheat normals to give illusion of **ADDITIONAL/FAKE** geometric detail*

# Bump Mapping

- Treat a **greyscale texture** as a single-valued height function
- Compute the normal from the partial derivatives in the texture

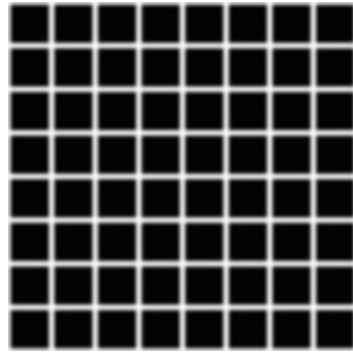


# Another Bump Map Example

---



**Cylinder w/Diffuse  
Texture Map**



**Bump Map**



**Cylinder w/Texture  
Map & Bump Map**



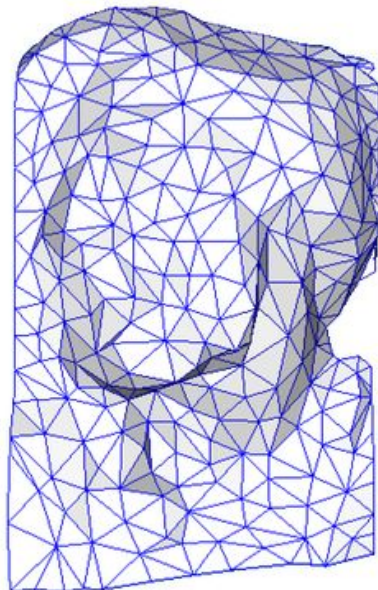
# Normal Mapping

[http://en.wikipedia.org/wiki/File:Normal\\_map\\_example.png](http://en.wikipedia.org/wiki/File:Normal_map_example.png)

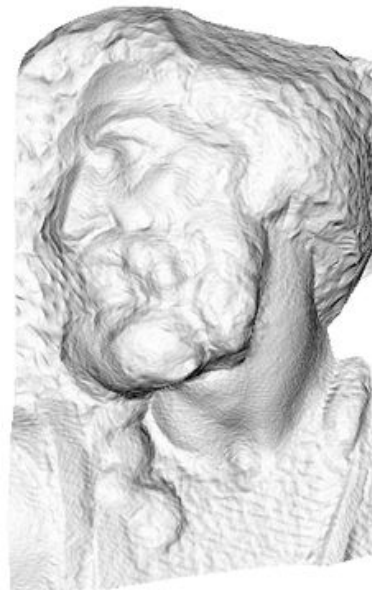
- Variation on Bump Mapping:  
Use an **RGB texture** to directly encode the normal



original mesh  
4M triangles



simplified mesh  
500 triangles

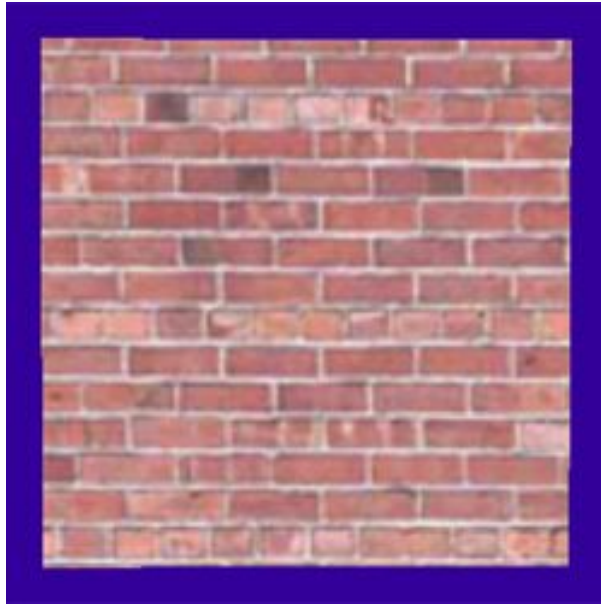


simplified mesh  
and normal mapping  
500 triangles

# What's Missing?

---

- There are no bumps on the silhouette of a bump-mapped or normal-mapped object
- Bump/Normal maps don't allow self-occlusion or self-shadowing



# Today

---

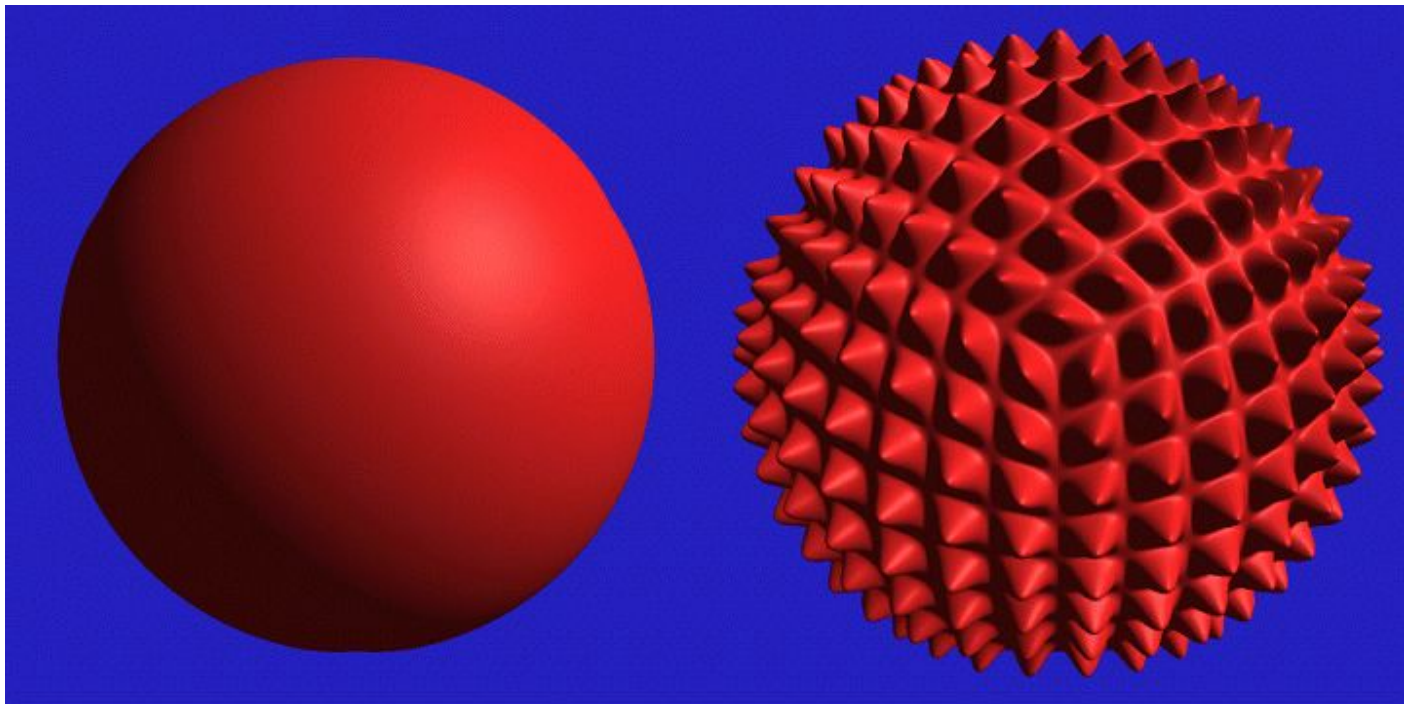
- Texture Mapping & Other “Mapping” Techniques
  - Bump Mapping
  - **Displacement Mapping**
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  - Light Mapping
  - Normal Mapping
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# Displacement Mapping

---

- Use the texture map to actually move the surface point
- The geometry must be displaced before visibility is determined

*Originally  
a CPU-only,  
post-user-  
modeling step*





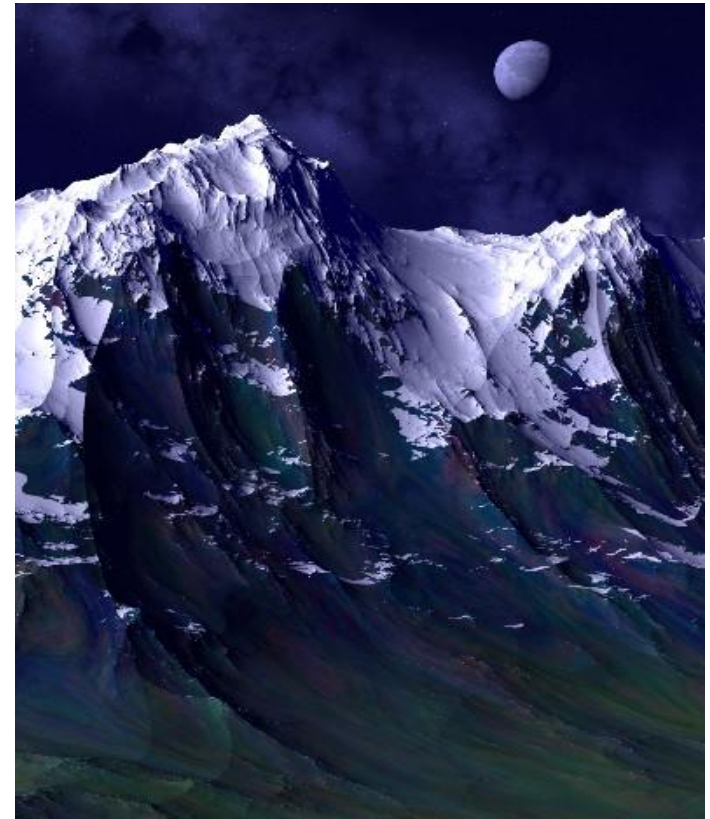
# Displacement Mapping

---

- “Geometry Caching for Ray-Tracing Displacement Maps”  
EGRW 1996. Pharr & Hanrahan
- *note the accurate and detailed shadows cast by the stones*



# Procedural Displacement Mapping



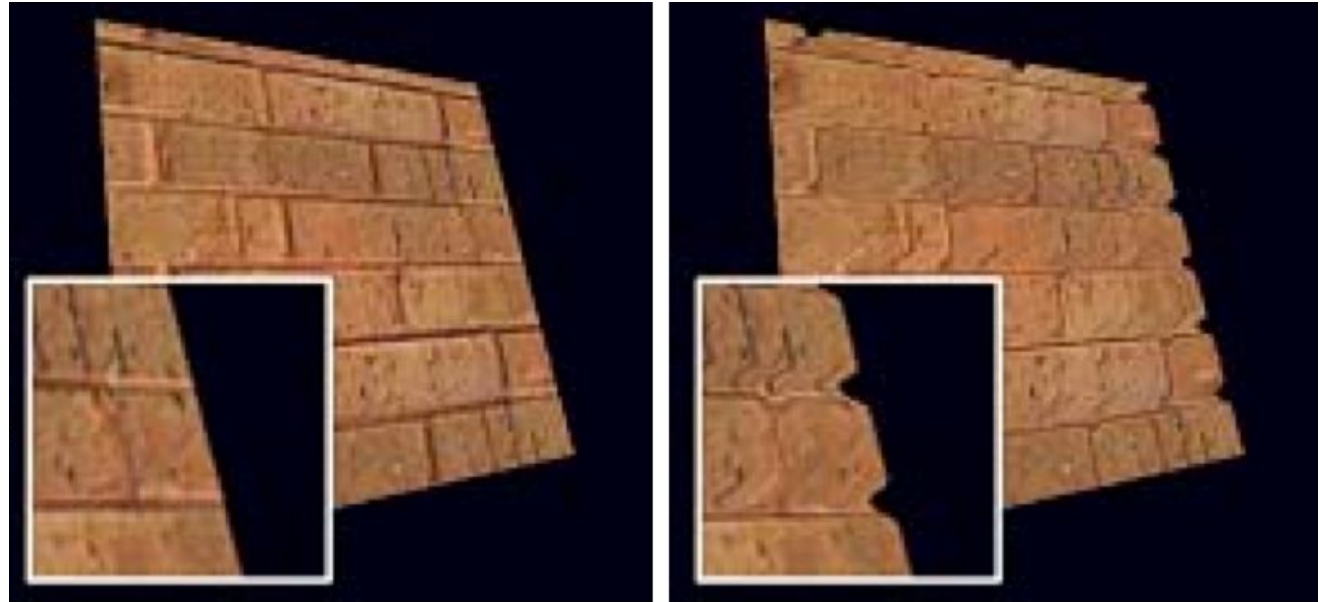
*Ken Musgrave* [www.kenmusgrave.com](http://www.kenmusgrave.com)

# Parallax Mapping

*a.k.a. Offset Mapping or  
Virtual Displacement Mapping*

- Displace the texture coordinates for each pixel based on view angle and value of the height map at that point
- At steeper view-angles, texture coordinates are displaced more, giving *illusion of depth* due to parallax effects

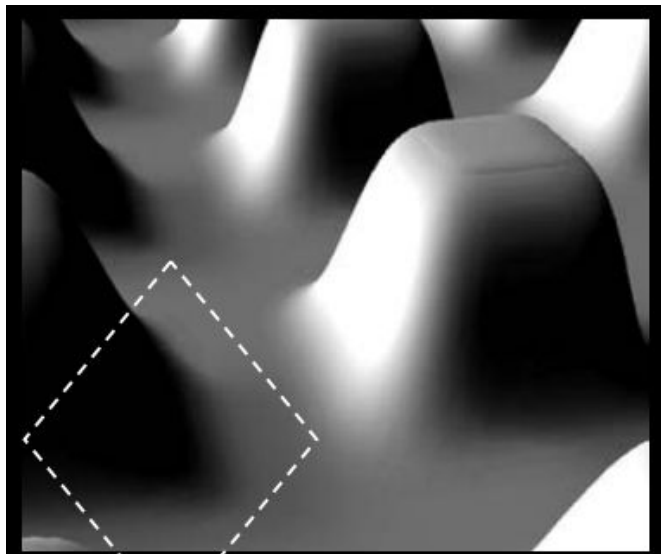
*“Detailed shape  
representation with  
parallax mapping”,  
Kaneko et al.  
ICAT 2001*



# Parallax Occlusion Mapping

---

- Brawley & Tatarchuk 2004
- Per pixel ray tracing of the heightfield geometry
- Occlusions & soft shadows



*[http://developer.amd.com/media/gpu\\_assets/  
Tatarchuk-ParallaxOcclusionMapping-Sketch-print.pdf](http://developer.amd.com/media/gpu_assets/Tatarchuk-ParallaxOcclusionMapping-Sketch-print.pdf)*



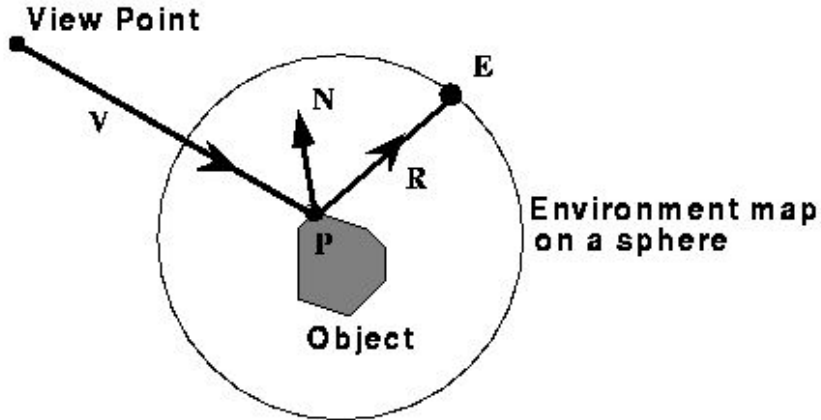
# Today

---

- Texture Mapping & Other “Mapping” Techniques
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# Environment Maps

- We can simulate reflections by using the direction of the reflected ray to index a spherical texture map at "infinity".
- Assumes that all reflected rays begin from the same point.



# What's the Best Chart?

*Box Map*



*Latitude Map*



*GL Map*





# Environment Mapping Example

*Terminator II*





# Texture Maps for Illumination

- Also called "Light Maps"



# Questions?

---

*Image by Henrik  
Wann Jensen*  
*Environment map  
by Paul Debevec*





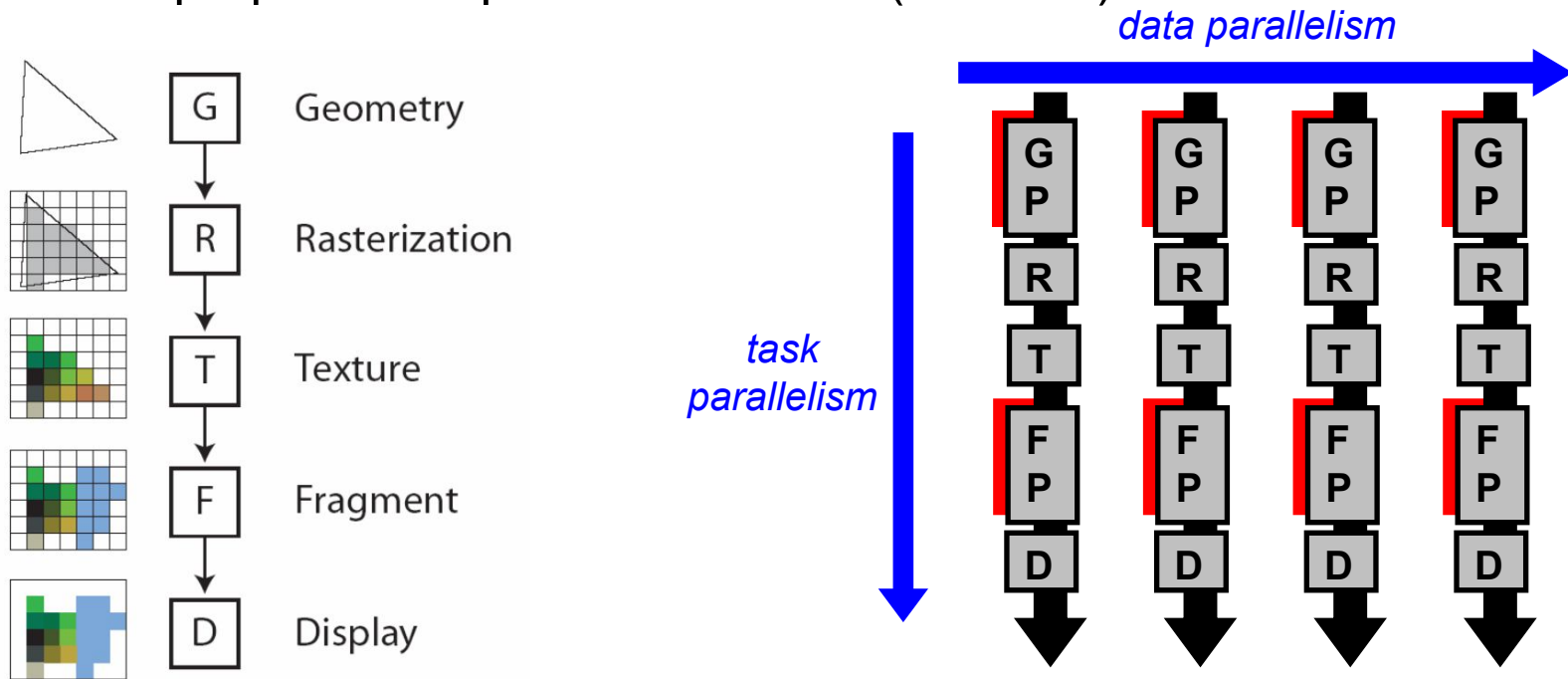
# Today

---

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# Modern Graphics Hardware

- Increased parallelism
- **Programmable** geometry and pixel/fragment stages
- General-purpose computation on GPU (GPGPU)





# GLSL example: hw4\_shader.vs

```
hw4_shader.vs
#version 330 core

// Input vertex data, different for all executions of this shader.
layout(location = 0) in vec3 vertexPosition_modelspace;
layout(location = 1) in vec3 vertexNormal_modelspace;
layout(location = 2) in vec3 vertexColor;

// Output data
out vec3 vertexPosition_worldspace;
out vec3 vertexNormal_worldspace;
out vec3 vertexNormal_cameraspace;
out vec3 EyeDirection_cameraspace;
out vec3 myColor;

// Values that stay constant for the whole mesh.
uniform mat4 MVP;
uniform mat4 V;
uniform mat4 M;
uniform vec3 LightPosition_worldspace;

void main(){

    // Output position of the vertex, in clip space : MVP * position
    gl_Position = MVP * vec4(vertexPosition_modelspace,1);

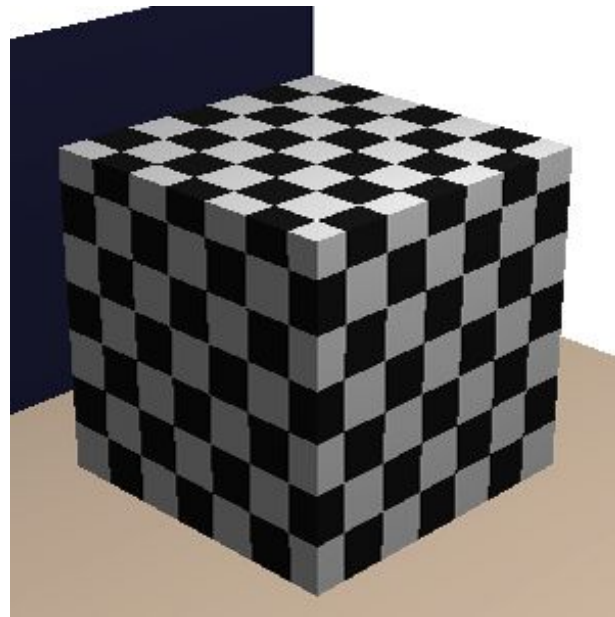
    // Position of the vertex, in worldspace : M * position
    vertexPosition_worldspace = (M * vec4(vertexPosition_modelspace,1)).xyz;

    // Vector that goes from the vertex to the camera, in camera space.
    // In camera space, the camera is at the origin (0,0,0).
    vec3 vertexPosition_cameraspace = ( V * M * vec4(vertexPosition_modelspace,1)).xyz;

    EyeDirection_cameraspace = vec3(0,0,0) - vertexPosition_cameraspace;

    vertexNormal_worldspace = normalize (M * vec4(vertexNormal_modelspace,0)).xyz;

    // pass color to the fragment shader
    myColor = vertexColor;
}
```



# GLSL example: hw4\_shader.fs

```
hw4_shader_checkerboard.fs
in vec3 vertexNormal_worldspace;

// Output data
out vec3 color;

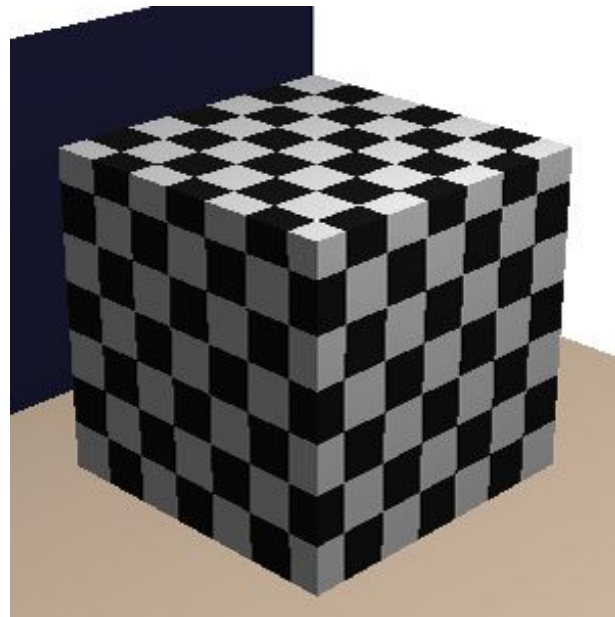
// Values that stay constant for the whole mesh.
uniform vec3 LightPosition_worldspace;
uniform int colormode;
uniform int whichshader;

// -----
// a shader for a black & white checkerboard
vec3 checkerboard(vec3 pos) {
    // determine the parity of this point in the 3D checkerboard
    int count = 0;
    if (mod(pos.x,0.3)> 0.15) count++;
    if (mod(pos.y,0.3)> 0.15) count++;
    if (mod(pos.z,0.3)> 0.15) count++;
    if (count == 1 || count == 3) {
        return vec3(0.1,0.1,0.1);
    } else {
        return vec3(1,1,1);
    }
}

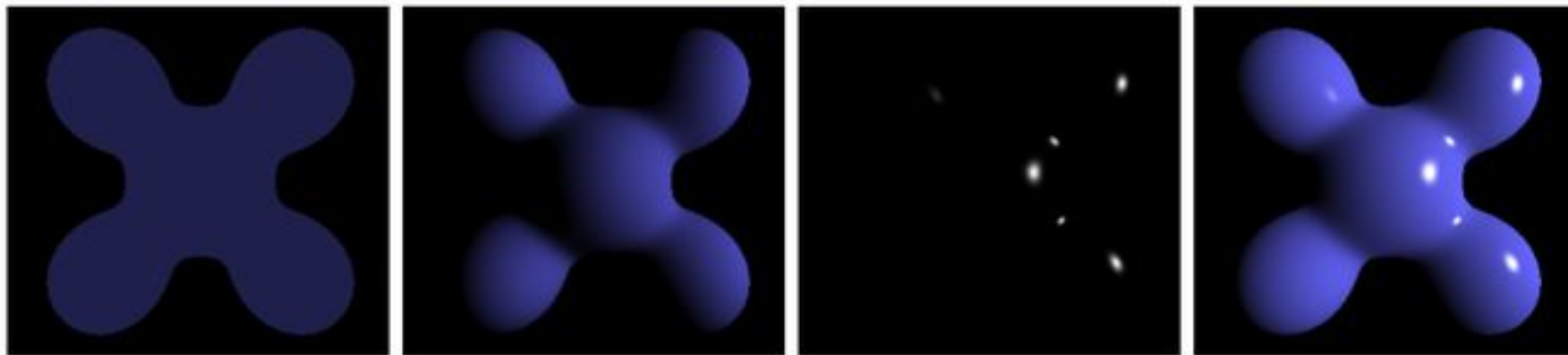
// -----
void main(){
    vec3 LightColor = vec3(1,1,1);
    float LightPower = 4.0f;

    // surface normal
    vec3 surface_normal = vertexNormal_worldspace;

    // Material properties
    vec3 MaterialDiffuseColor = myColor;
    if (whichshader == 1) {
        MaterialDiffuseColor = checkerboard(vertexPosition_worldspace);
    } else if (whichshader == 2) {
        vec3 normal2;
        MaterialDiffuseColor = orange(vertexPosition_worldspace,surface_normal);
    } else if (whichshader == 3) {
        MaterialDiffuseColor = wood(vertexPosition_worldspace,surface_normal);
    }
}
```



# Phong Reflection/Lighting Model



Ambient

+

Diffuse

+

Specular

=

Phong Reflection

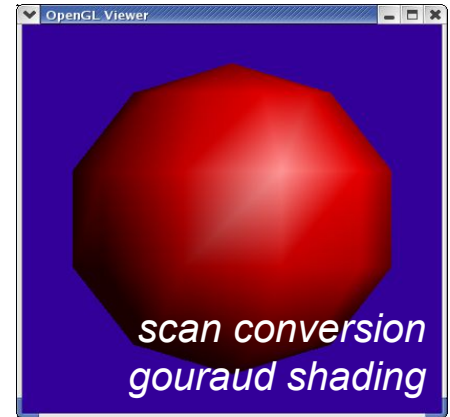
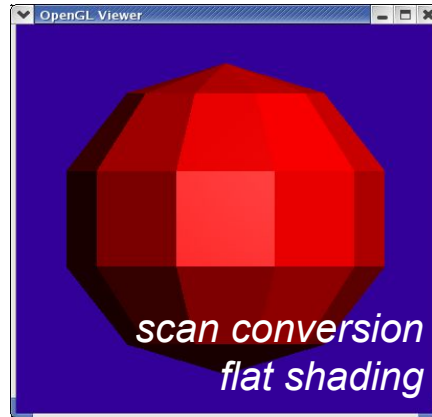
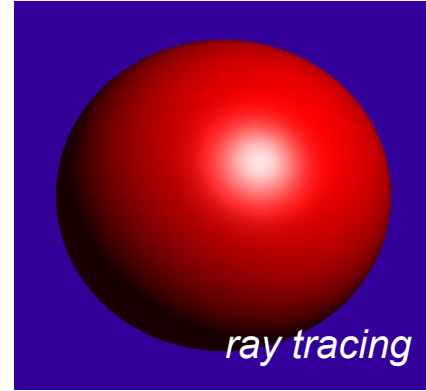
$$I_p = k_a i_a + \sum_{m \in \text{lights}} (k_d (\hat{L}_m \cdot \hat{N}) i_{m,d} + k_s (\hat{R}_m \cdot \hat{V})^\alpha i_{m,s})$$

# Color & Normal Interpolation

- It's easy in OpenGL to specify different colors and/or normals at the vertices of triangles:
- Why is this useful?



*Originally, all we could afford to do in hardware was interpolate colors*

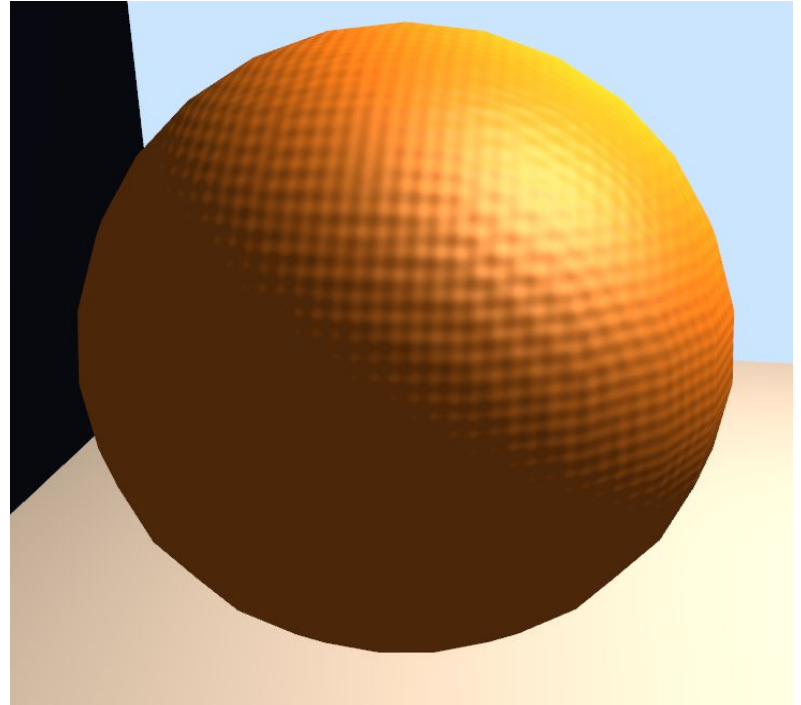
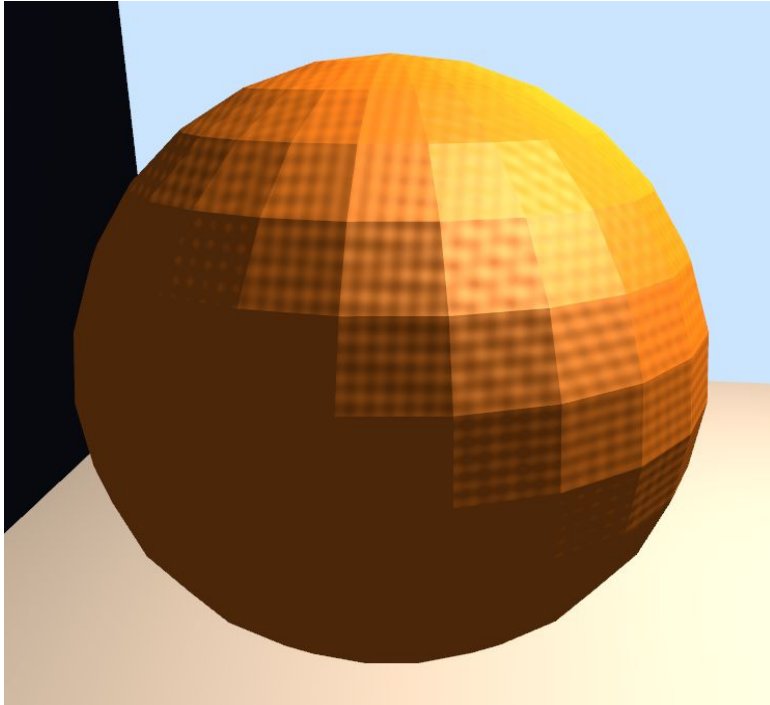




# Per-Pixel Shading!

---

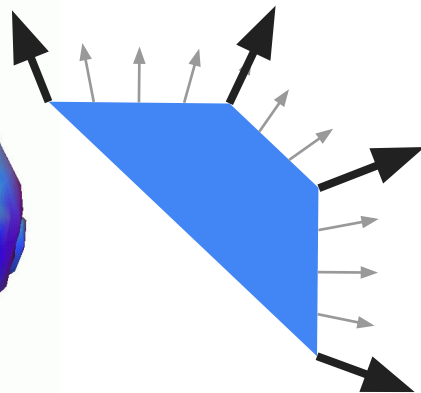
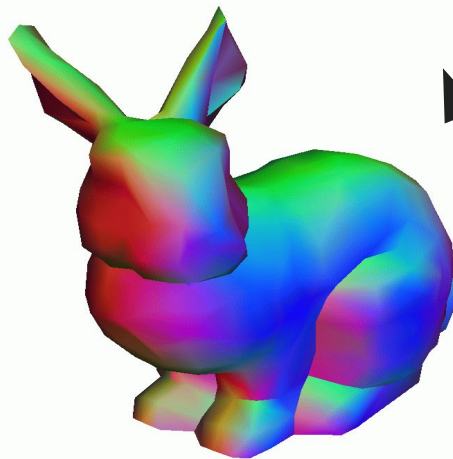
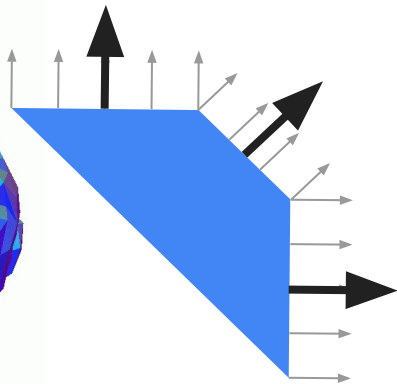
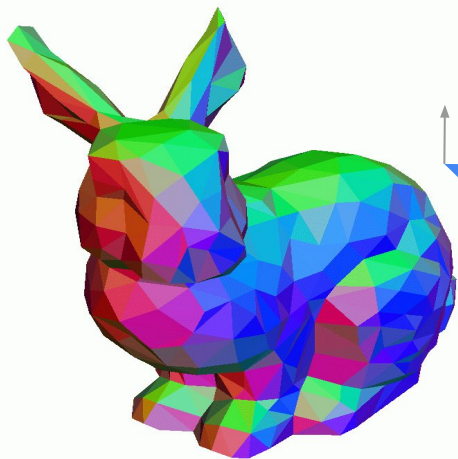
- We are not just interpolating the color
- Phong Reflection/Lighting can be calculated per pixel, not just per vertex



# Phong Normal Interpolation

(Not Phong *Shading*)

- *Interpolate the average vertex normals* across the face and compute *per-pixel shading*
  - Normals should be re-normalized (ensure length=1)
- Before shaders, per-pixel shading was not possible in hardware (Gouraud shading is actually a decent substitute!)



# Another GLSL example: orange.vs

```
Emacs@tony.dyn.cs.rpi.edu
varying vec3 normal;
varying vec3 position_eyespace;
varying vec3 position_worldspace;

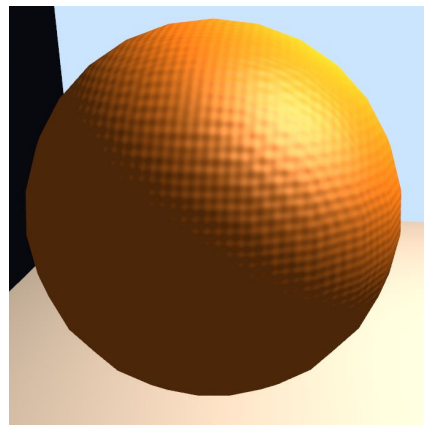
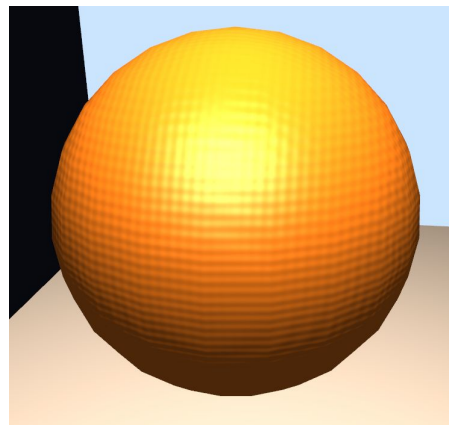
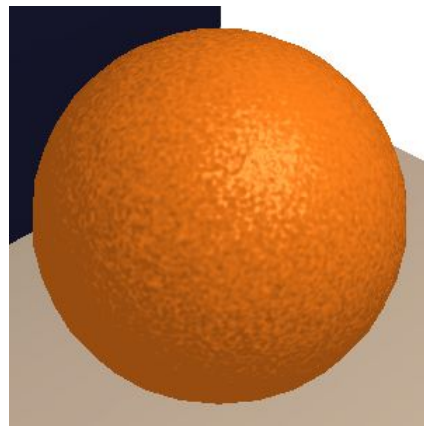
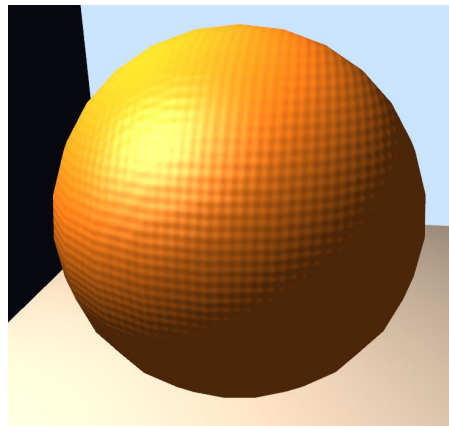
// a shader that looks like orange peel

void main(void) {

    // the fragment shader requires both the world space position (for
    // consistent bump mapping) & eyespace position (for the phong
    // specular highlight)
    position_eyespace = vec3(gl_ModelViewMatrix * gl_Vertex);
    position_worldspace = gl_Vertex.xyz;

    // pass along the normal
    normal = normalize(gl_NormalMatrix * gl_Normal);

    gl_Position = gl_ModelViewProjectionMatrix * gl_Vertex;
}
```



# Another GLSL example: orange.fs

```
Emacs@tony.dyn.cs.rpi.edu

varying vec3 normal;
varying vec3 position_eyespace;
varying vec3 position_worldspace;

// a shader that looks like orange peel

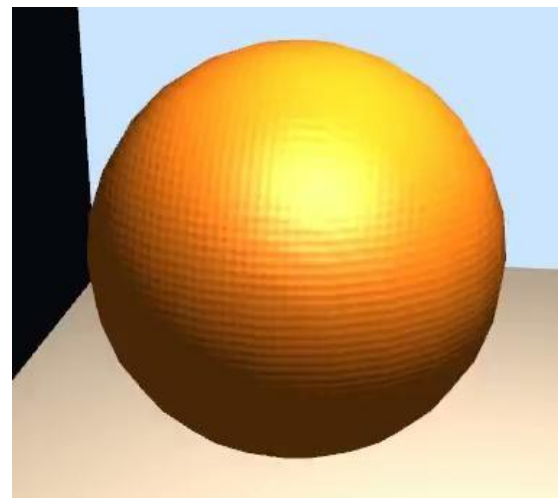
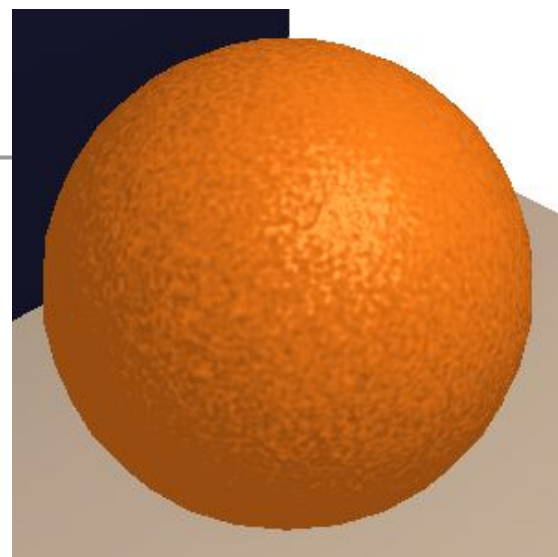
void main (void) {

    // the base color is orange!
    vec3 color = vec3(1.0,0.5,0.1);

    // high frequency noise added to the normal for the bump map
    vec3 normal2 = normalize(normal+0.4*noise3(70.0*position_worldspace));

    // direction to the light
    vec3 light = normalize(gl_LightSource[1].position.xyz - position_eyespace);
    // direction to the viewer
    vec3 eye_vector = normalize(-position_eyespace);
    // ideal specular reflection
    vec3 reflected_vector = normalize(-reflect(light,normal2));

    // basic phong lighting
    float ambient = 0.6;
    float diffuse = 0.4*max(dot(normal2,light),0.0);
    float specular = 0.2 * pow(max(dot(reflected_vector,eye_vector),0.0),10.0);
    vec3 white = vec3(1.0,1.0,1.0);
    color = ambient*color + diffuse*color + specular*white;
    gl_FragColor = vec4 (color, 1.0);
}
```



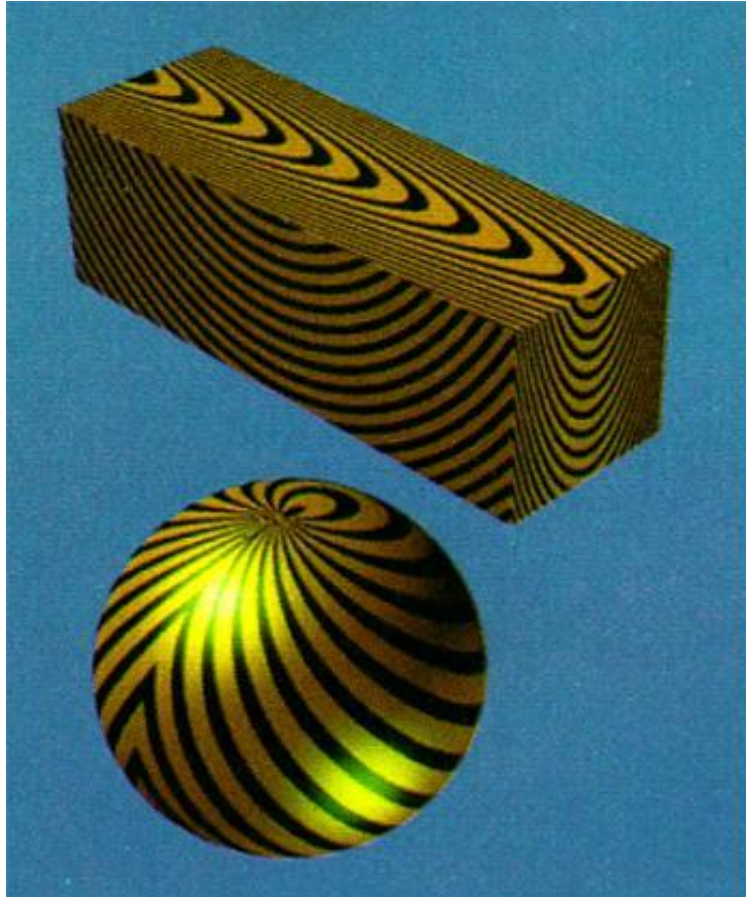


# Today

---

- Texture Mapping & Other “Mapping” Techniques
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# Texture Map vs. Solid Texture

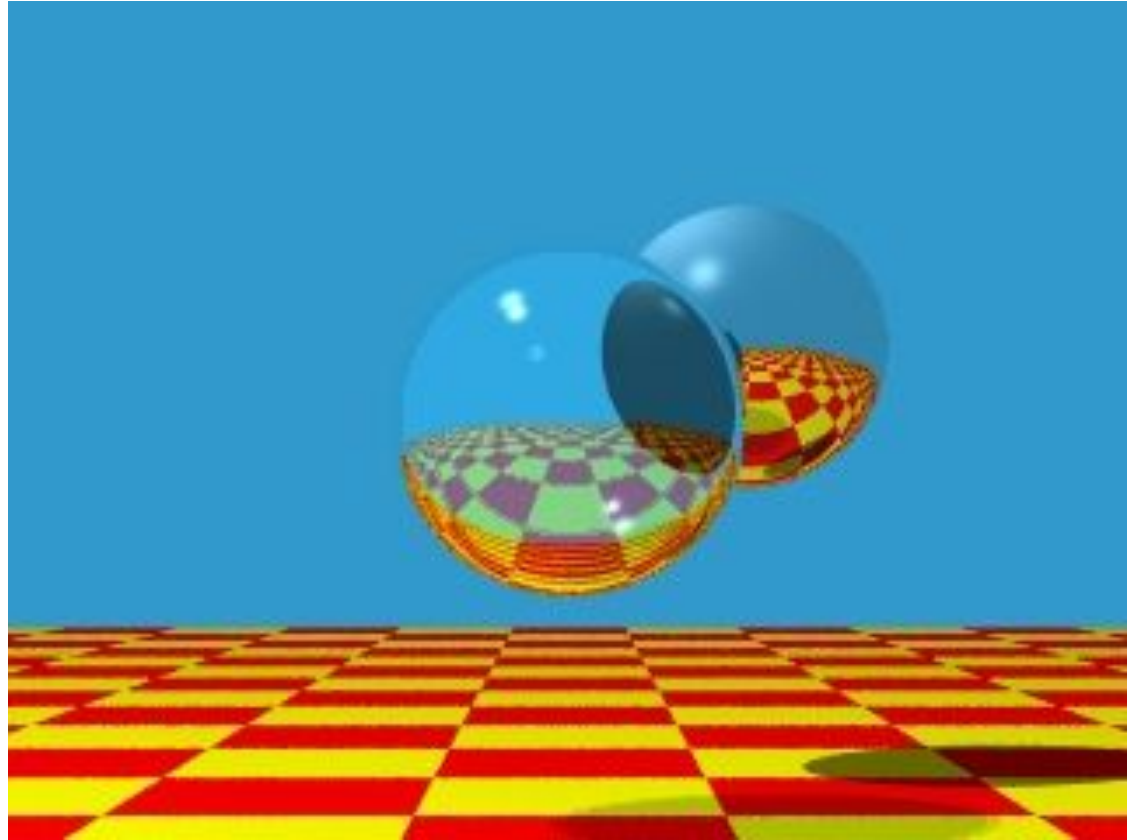


“Solid Texturing of  
Complex Surfaces”,  
Peachey,  
SIGGRAPH 1985

# Procedural Textures

---

$f(x,y,z) \rightarrow color$

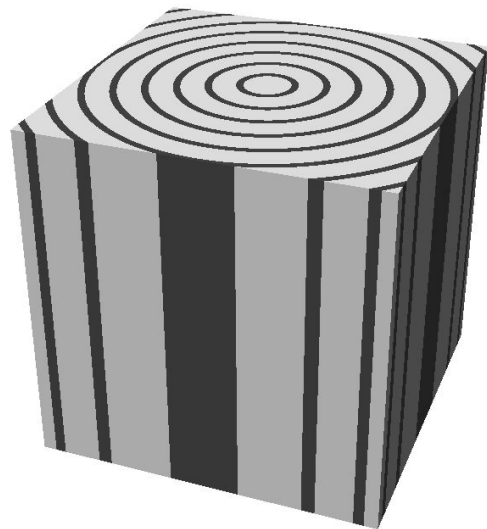
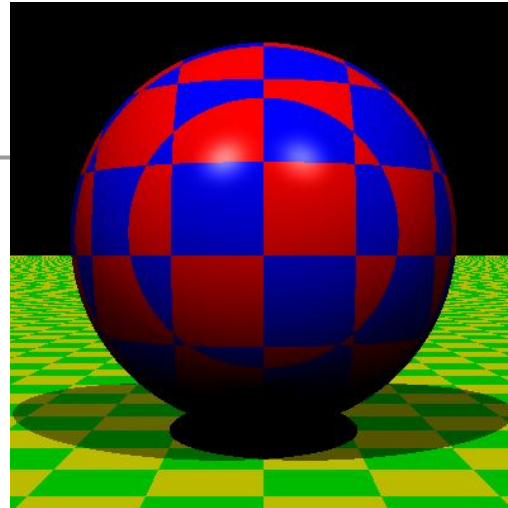


*Image by Turner Whitted*

# Procedural Textures

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- Advantages:
  - easy to implement in ray tracer
  - more compact than texture maps (especially for solid textures)
  - infinite resolution
- Disadvantages
  - non-intuitive
  - difficult to match existing texture





# Today

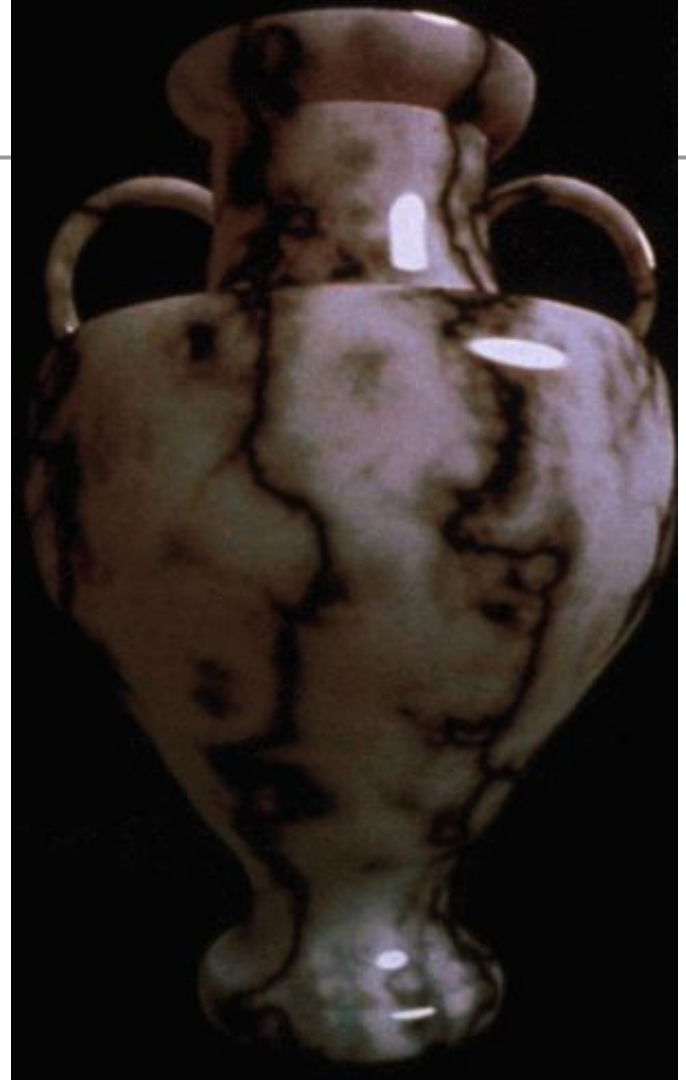
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- Texture Mapping & Other “Mapping” Techniques
  - Bump Mapping
  - Displacement Mapping
  - Environment Mapping
  - Light Mapping
  - Normal Mapping
  - Parallax Mapping
  - Parallax Occlusion Mapping
- Programmable Shader Examples
  - Modern Graphics Hardware
  - Per-Pixel Shading
- Procedural Textures & Modeling
- **Papers for Today**
- Papers for Next Time

# Reading for Today

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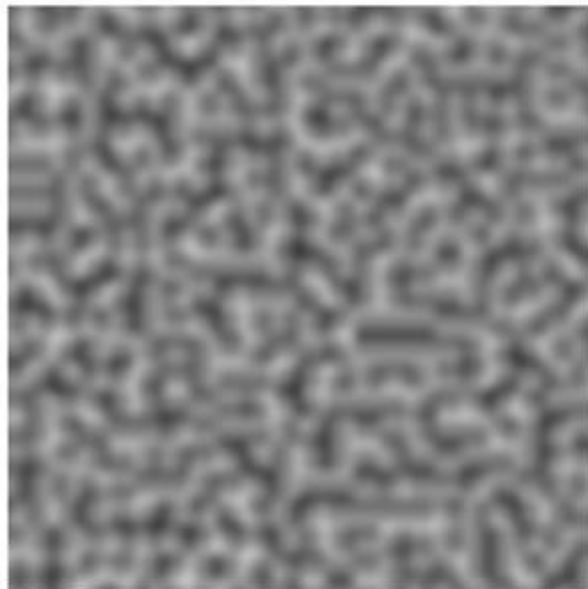
- “An Image Synthesizer”, Perlin, SIGGRAPH 1985 – *and* –
- “Improving Noise”, Perlin, SIGGRAPH 2002



# Perlin Noise

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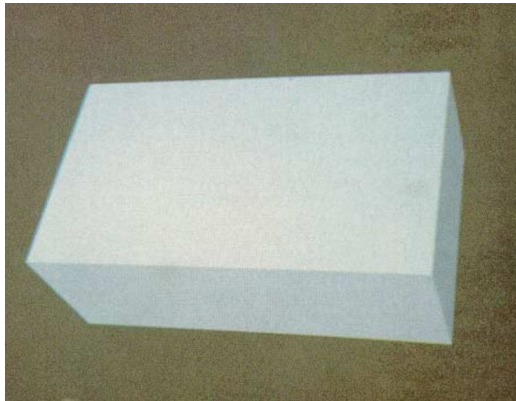
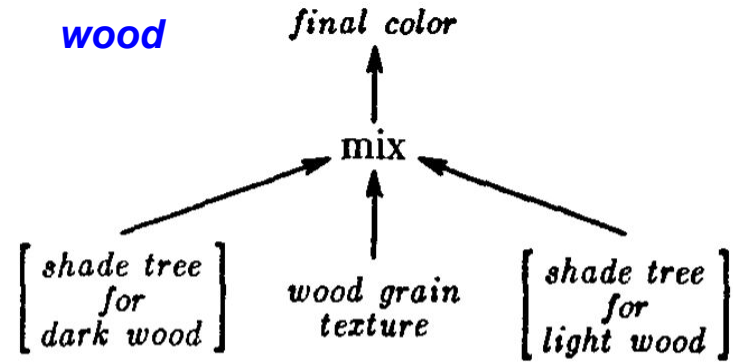
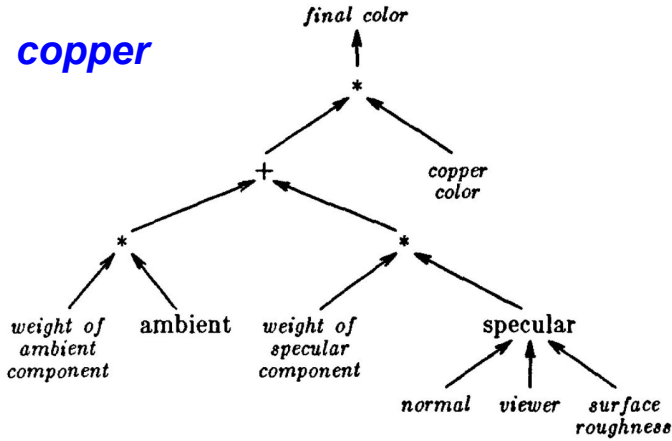
- Properties:
  - Looks “random”, but is deterministic (always returns the same answer for a specific coordinate)
  - Small memory footprint & fast to compute
  - Known amplitude & frequency
  - Smooth interpolation when zoomed in
- Can be combined/layered:
  - Add multiple noise functions w/ different frequencies and amplitudes
  - Simple arithmetic operations (thresholding, sine waves, etc.)



- Clear motivation & methodology,
  - Even distribution, prevent clumping, avoid struggle with UV mapping
  - Focus on efficiency, minimize memory/storage, unlimited resolution
- Use of a hash function for noise was interesting
  - Complex patterns from simple math
- Versatile - 1D or 2D or 3D (or higher), lots of example uses (excessive?)
- What is “realistic”? Not actually a scientifically provable thing!
  - How do we know its good? It “looks good”?
- More casual paper style
- 2 page paper fixing a flaw in original algorithm is interesting  
(unsure/unclear about the actual necessity / difference in the output)

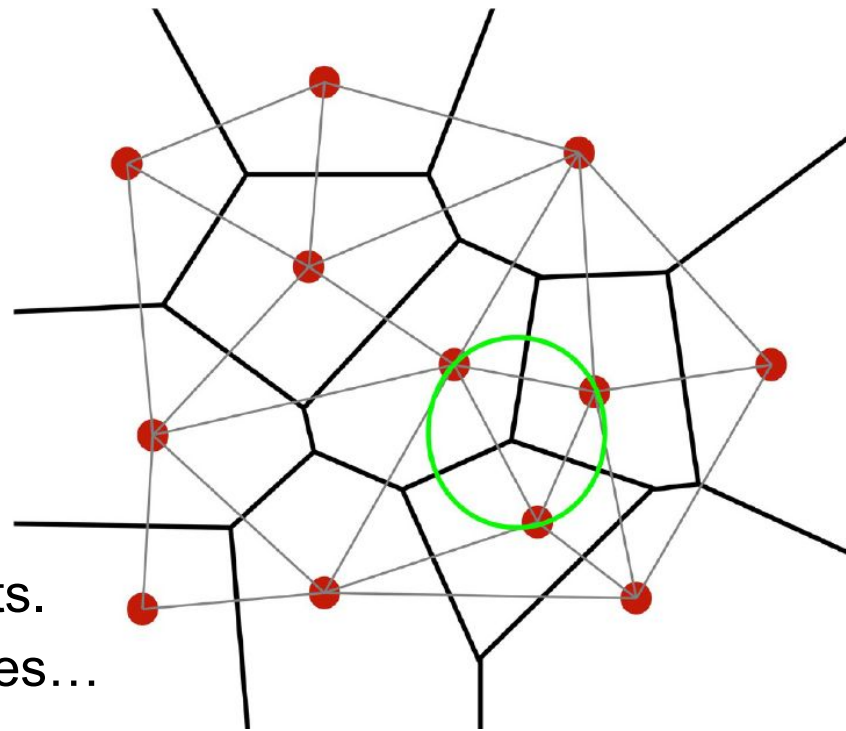


# “Shade Trees”, Cook, SIGGRAPH 1984



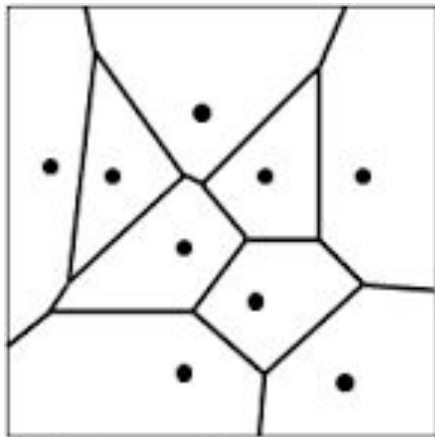
- **Grey: Delaunay Triangulation**

- “Best” triangulation of the red dots (most equilateral)
- A specific triangle is in the Delaunay Triangle *if and only if* the circle defined by those 3 points *does not* contain any other red dot
- Note: Well defined for random points. Points on a uniform grid will have ties...

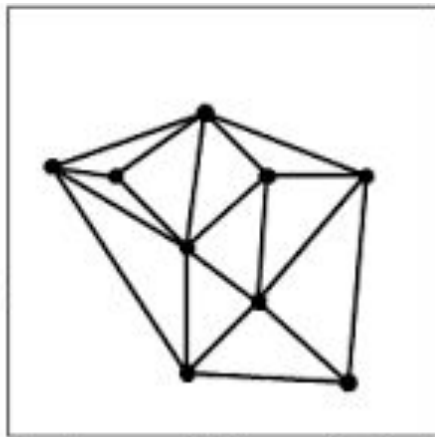


- **Black: Voronoi Diagram**

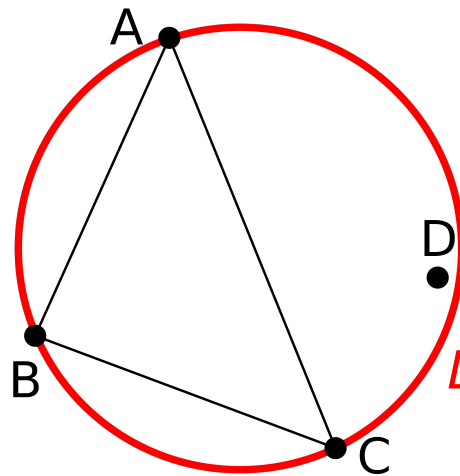
- Each cell is the set of all points in the plane that claim that cell's red dot as the closest
- *Note: The black edges perpendicularly bisect the grey edges*



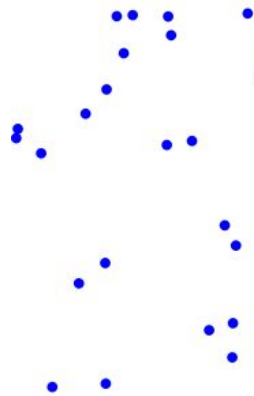
Voronoi Diagram



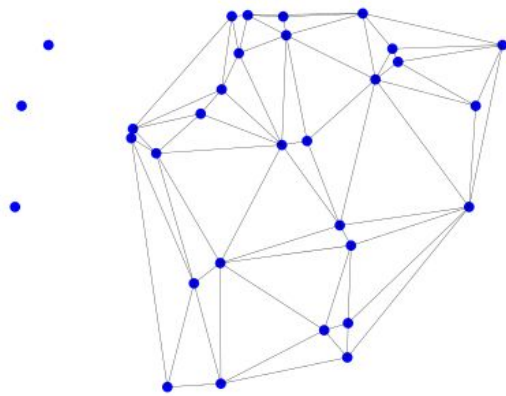
Delaunay Triangulation



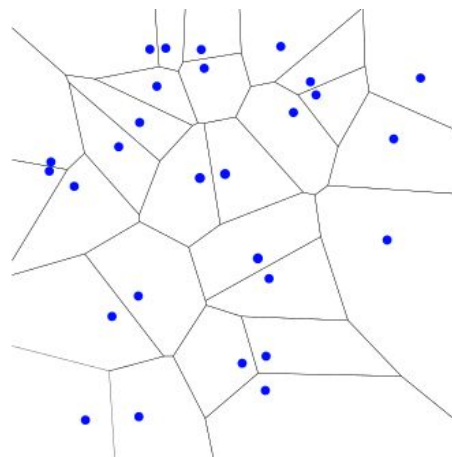
*invalid  
Delaunay  
triangle*



Input



Delaunay Triangulation

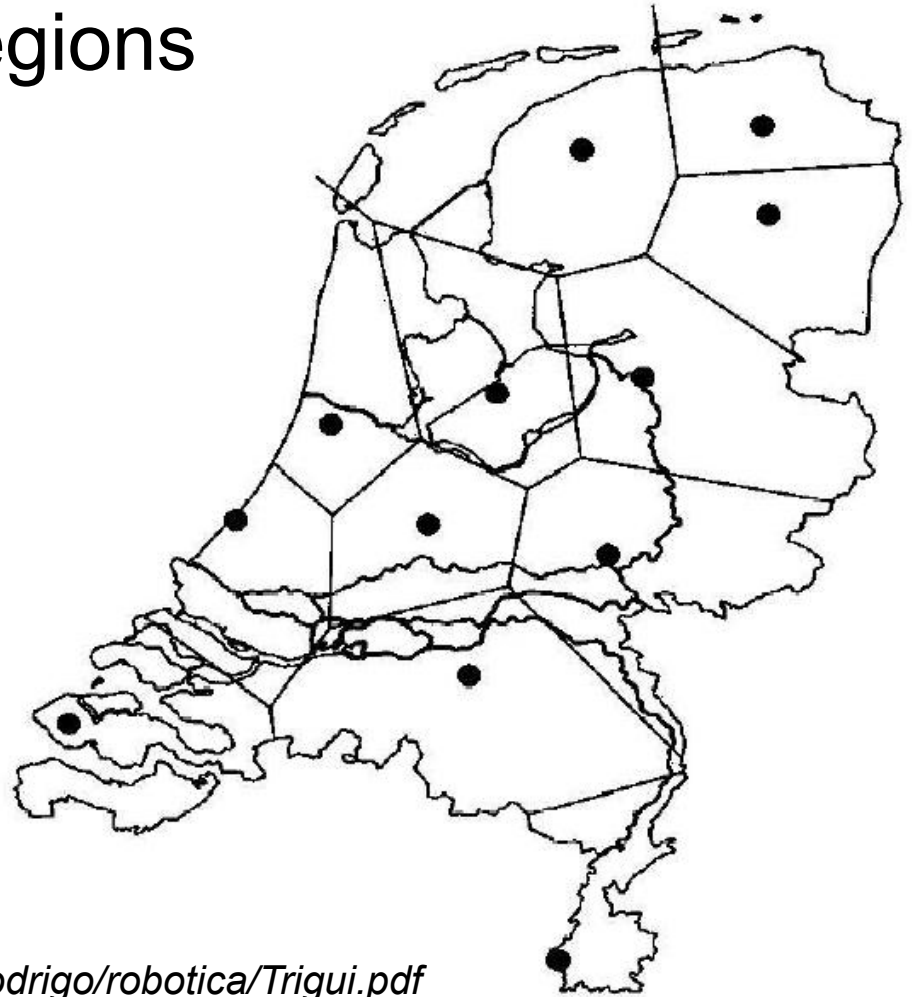


Voronoi Diagram

# Voronoi Diagram/Cells/Regions

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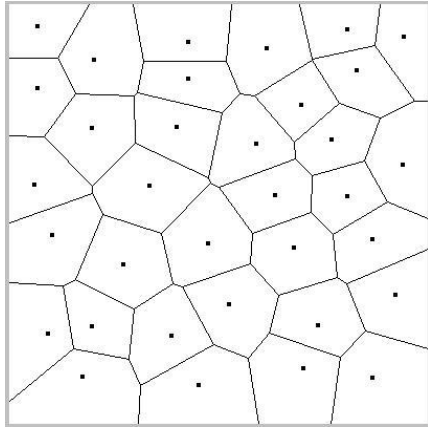
- How to re-district the Netherlands into provinces so that everyone reports to the closest capital
- Cell edges are the perpendicular bisectors of nearby points
- 2D or 3D
- Supports efficient *Nearest Neighbor* queries



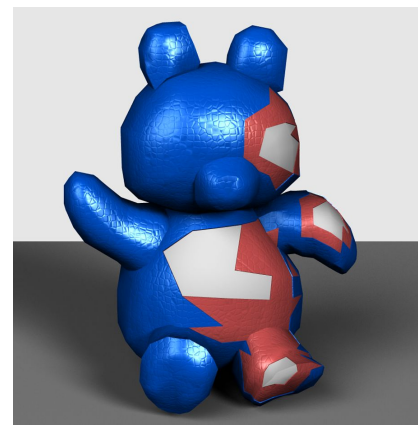
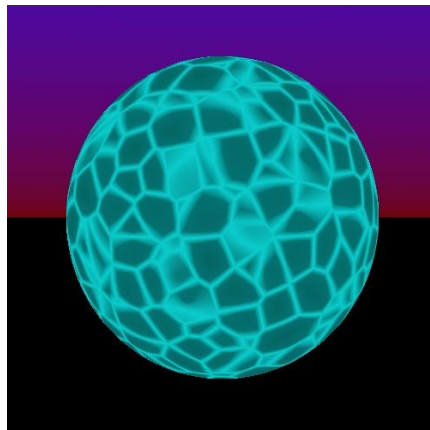
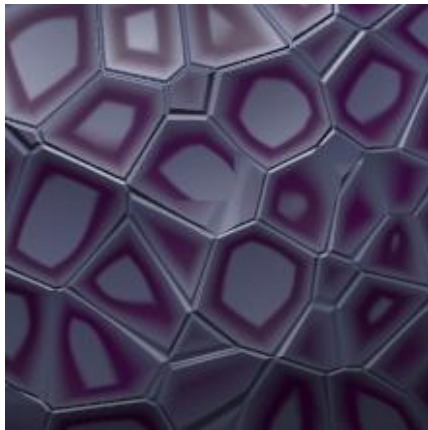


# Cellular Textures (using a Voronoi Diagram!)

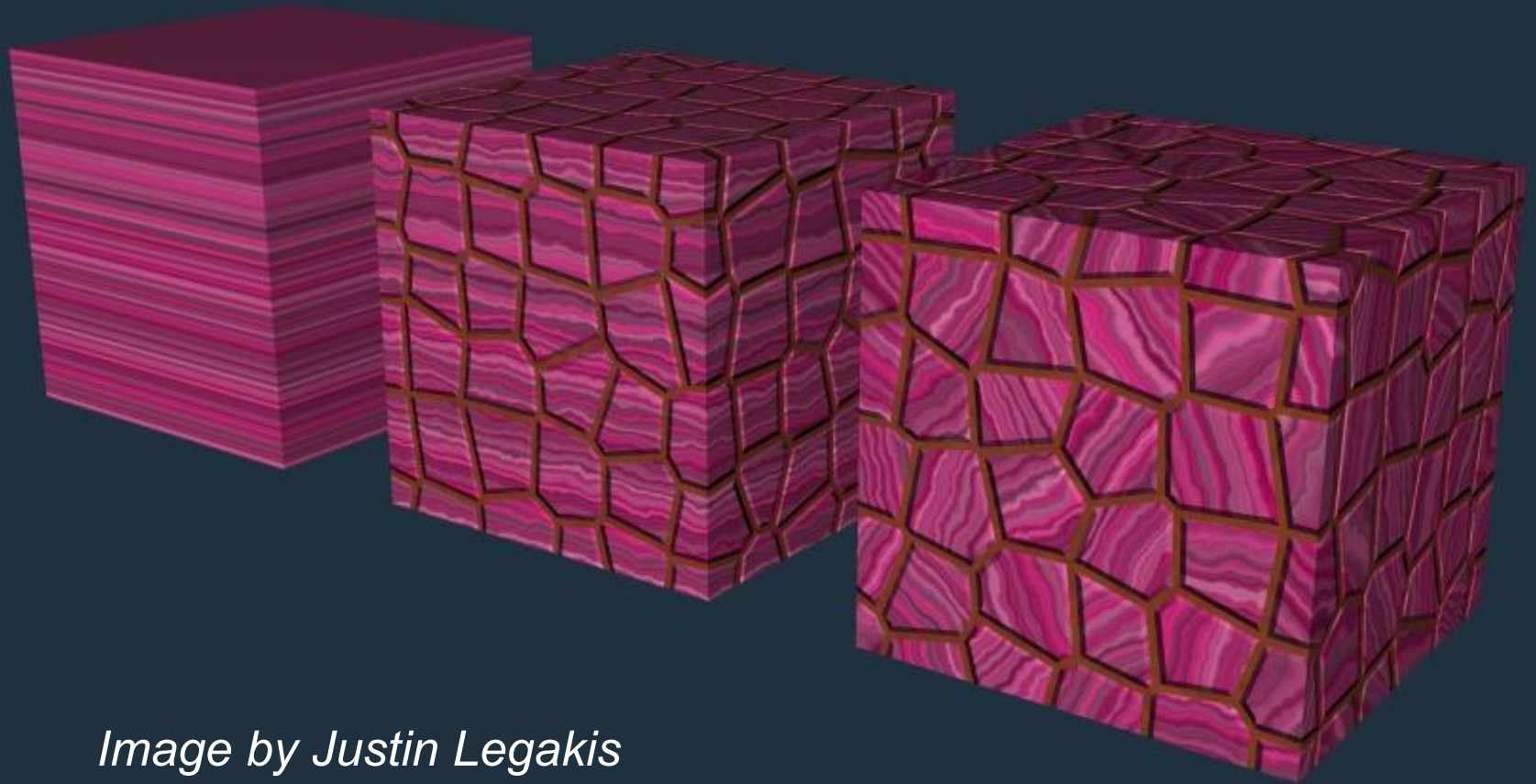
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*“A Cellular Texture Basis Function”,  
Worley, SIGGRAPH 1996  
[www.worley.com](http://www.worley.com)*



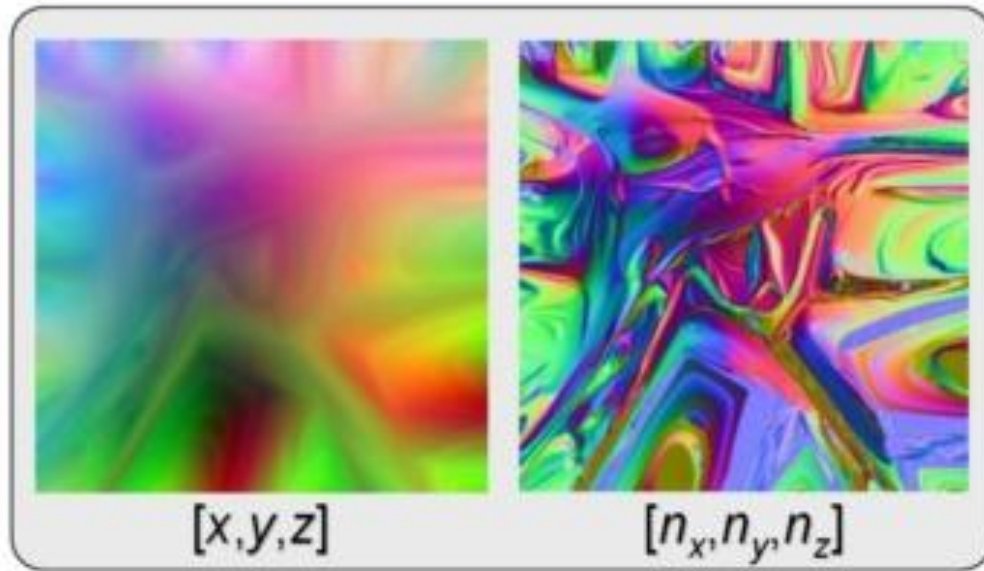
# Questions?



*Image by Justin Legakis*

# Optional Reading for Today

- "Geometry Images", Gu, Gortler, & Hoppe, SIGGRAPH 2002
- 3D shape is unrolled/flattened/stretched into a square image.
- Stored using existing image formats and compression methods.





# Optional Reading for Today

- “Hardware-Accelerated Global Illumination by Image Space Photon Mapping” McGuire & Luebke, HPG 2009

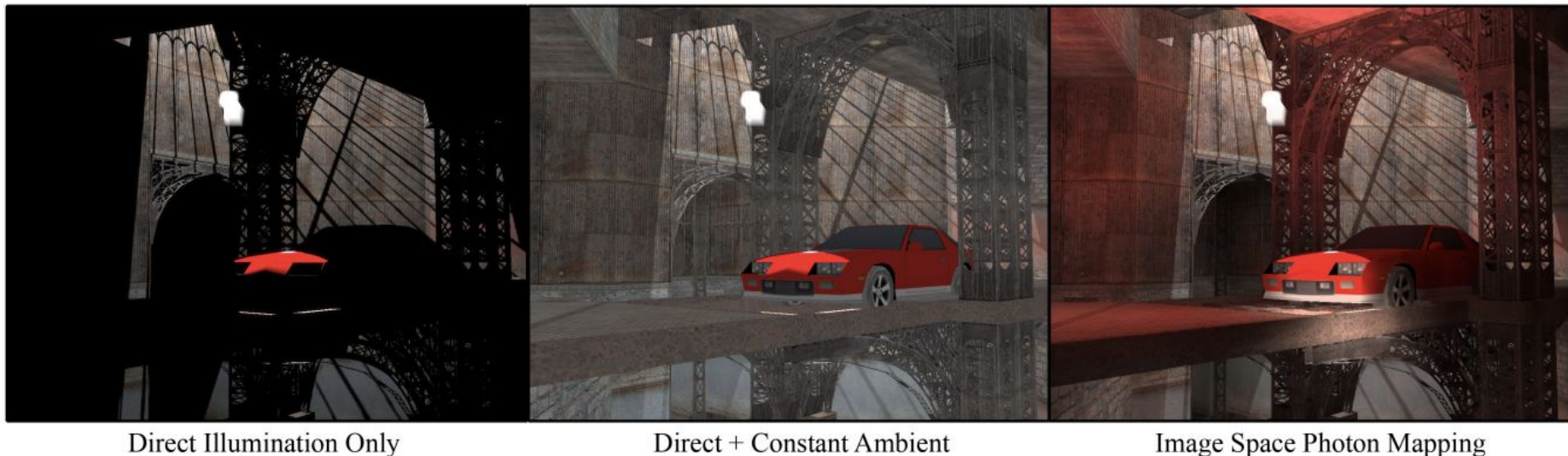
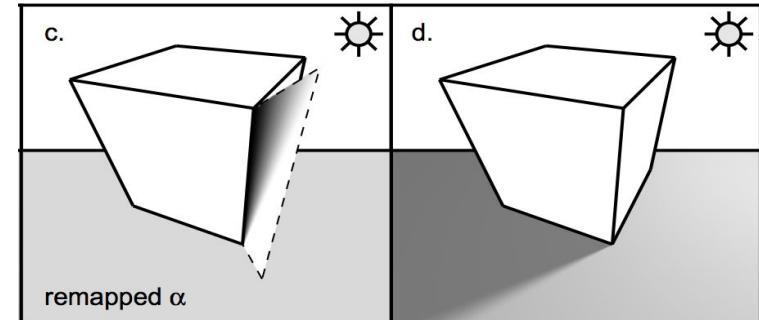
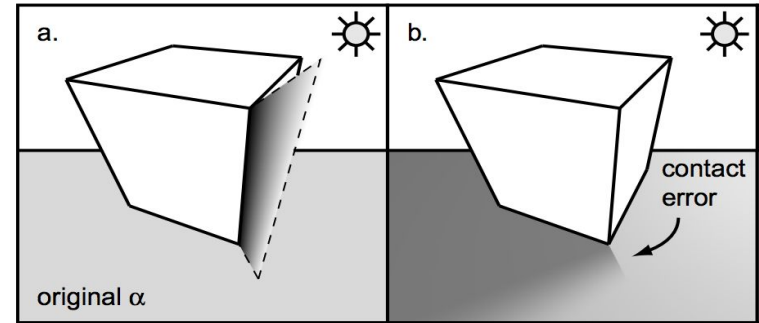
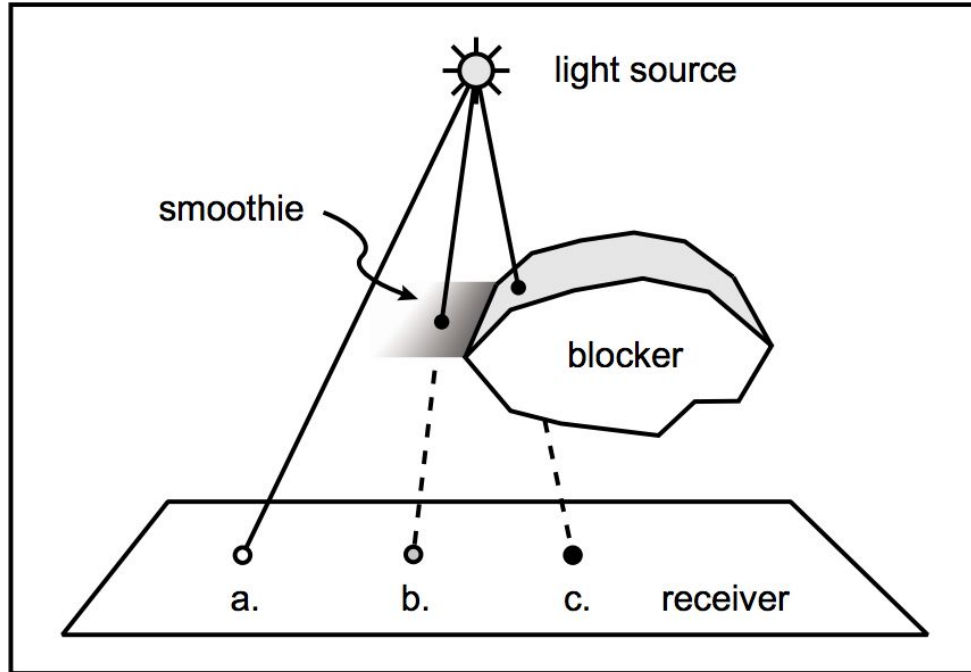


Figure 1: Image-space photon mapping can compute global illumination at interactive rates for scenes with multiple lights, caustics, shadows, and complex BSDFs. This scene renders at 26 Hz at  $1920 \times 1080$ . (Indirect and ambient intensity are amplified for comparison in this image.)



# Reading for Last Time

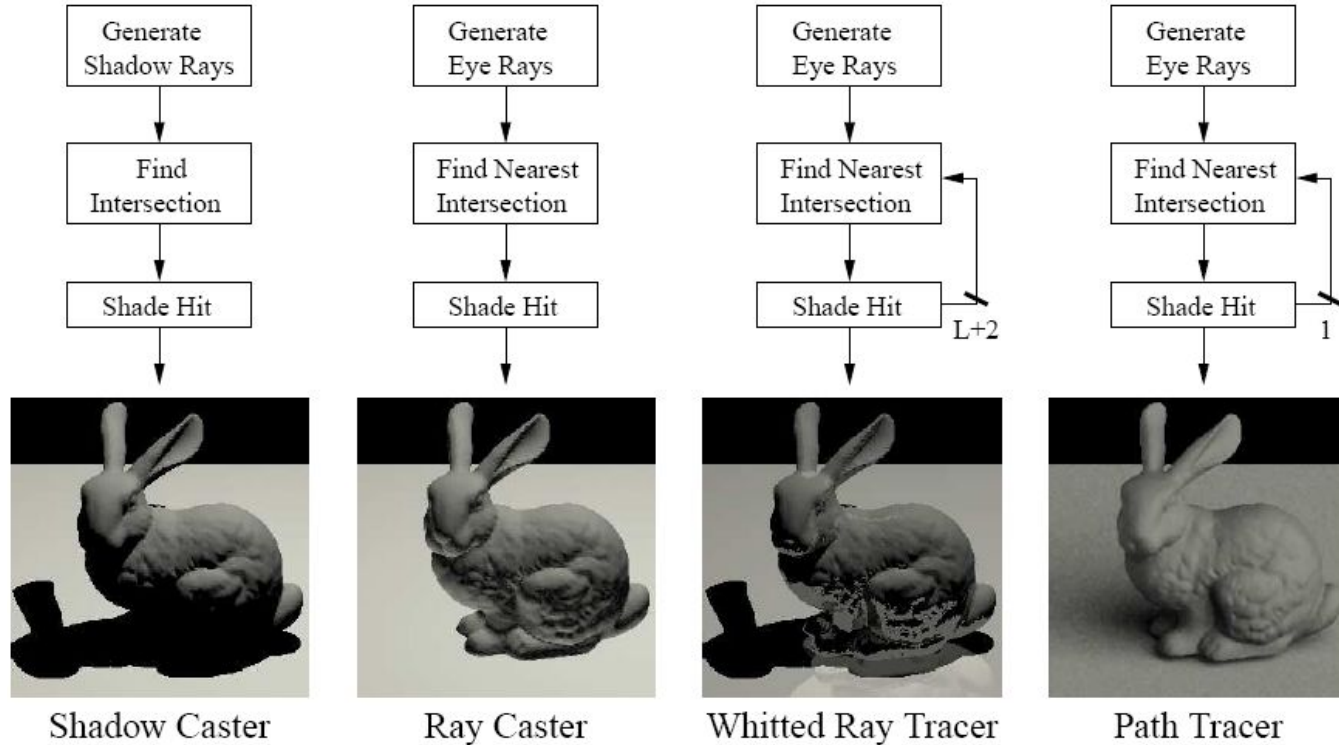
- "Rendering Fake Soft Shadows with Smoothies", Chan & Durand, EGSR 2003



- Interesting to read how hardware capabilities have evolved over years
  - Do researchers plan/think ahead about algorithms for future hardware
- creative/unexpected solution
- Seems expensive for a scene with moving objects (must recompute silhouette edges)
- Limitations on specific shape of light source
- Just because an algorithm is a 'hack' doesn't mean its without use/purpose - for the right scene & application its great

# Reading for Last Time

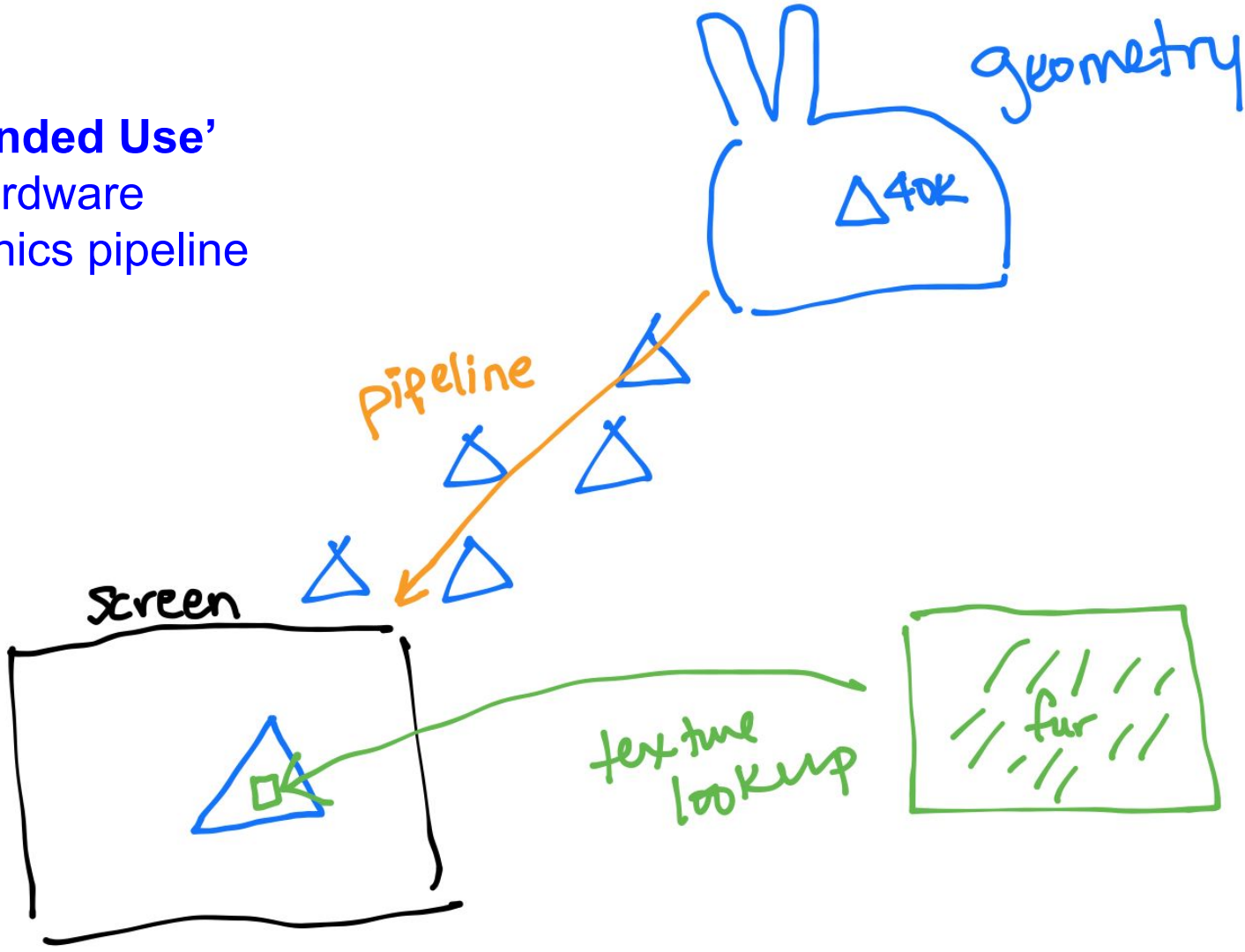
- “Ray Tracing on Programmable Graphics Hardware”, Purcell, Buck, Mark, & Hanrahan SIGGRAPH 2002



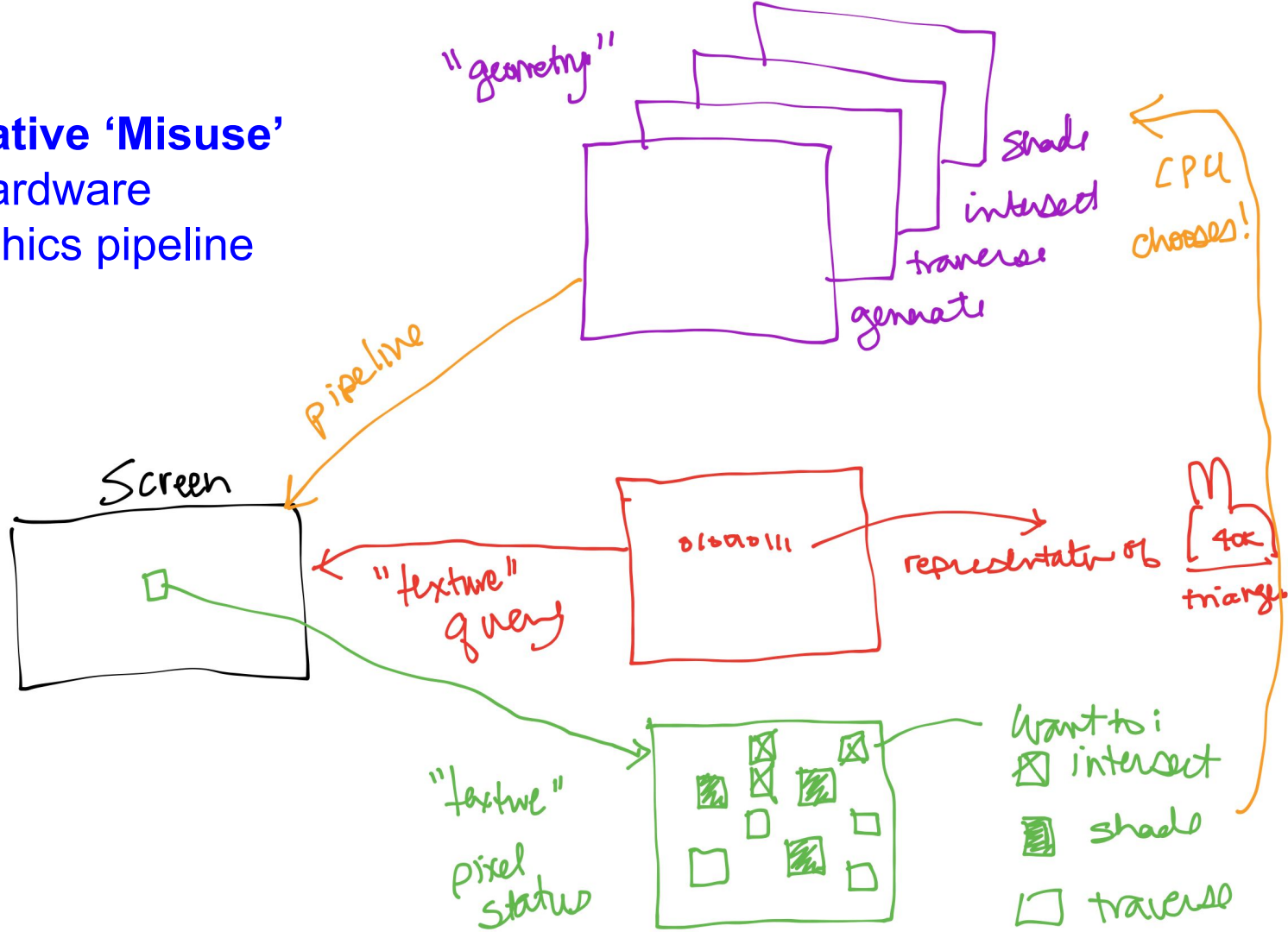
- In order to write best software, you must understand the hardware.  
In order to create best hardware, you must understand the software.
- How long were they waiting for this hardware? When did they first imagine that this would be possible with upcoming hardware?
- Interesting how the evolution of graphics hardware: fixed function → programmable → now returning to fixed function/non programmable
- Moore's law, variation in relative development rates of GPU vs CPU



**'Intended Use'**  
of hardware  
graphics pipeline



# Creative 'Misuse' of hardware graphics pipeline



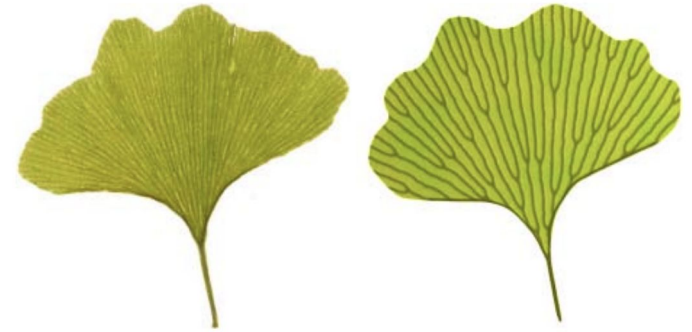
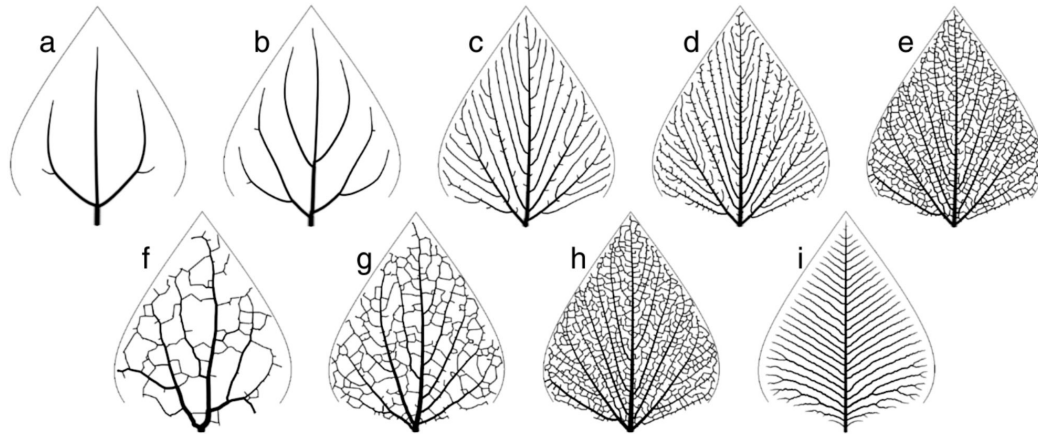
# Today

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- Texture Mapping & Other “Mapping” Techniques
  - Bump Mapping
  - Displacement Mapping
  - Environment Mapping
  - Light Mapping
  - Normal Mapping
  - Parallax Mapping
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- Procedural Textures & Modeling
- Papers for Today
- **Papers for Next Time**

# Papers for Next Time (*pick one*)

- “Modeling and visualization of leaf venation patterns”, Runions, Fuhrer, Lane, Federl, Roggan-Lagan, & Prusinkiewicz, 2007.



**Figure 10:** A photograph (left) and a rendered model of ginkgo venation (right).



**Figure 11:** A photograph(left) and a rendered model of lady's mantle venation (right).



# Papers for Next Time (*pick one*)

- “Procedural Modeling of Cities”,  
Parish & Müller,  
SIGGRAPH 2001

